Introducción a la Fotografia 3D UBA/FCEN Marzo 27 – Abril 12 2013 Clase 1 : Miercoles Marzo 27

Gabriel Taubin
Brown University



3D Shapes

- Industry
 - Reverse engineering
 - Fast metrology
 - Physical simulations
- Entertainment
 - Animating digital clays for movies or games
- Archeology and Art
 - Digitization of cultural heritage and artistic works
- Medical Imaging
 - Visualization
 - Segmentation



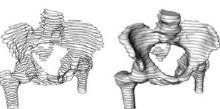
















Que es la Fotografia 3D?

Metodos y sistemas para capturar la geometria y la apariencia de objetos tridimensionales, basados en el uso de camaras y fuentes de luz

3D Photography

Laser Scanning

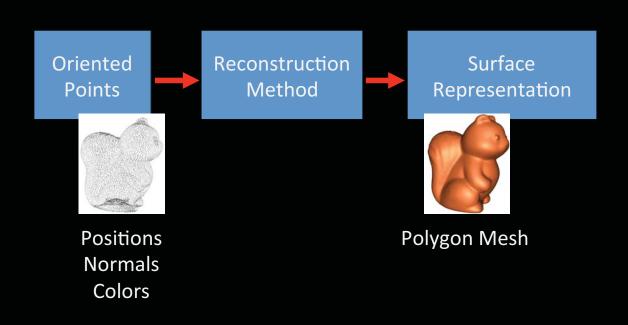
Coriented
Points

Structured Lighting

Multi-View Stereo

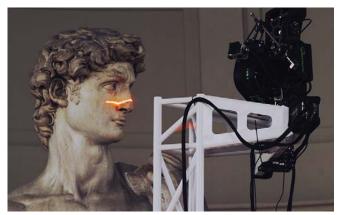
Positions, Normals, Colors

Surface Reconstruction



Followed by Geometry Processing (Next Course)

3D Shape and Appearance Capture



Laser range scanning devices



Multi-camera systems









Structured lighting systems

Objetivos

Adquirir conocimientos básicos sobre:

- Métodos y sistemas para la captura, reconstrucción y procesamiento de objetos en 3D
- Fundamentos Matemáticos, en particular de métodos basados en cámaras y proyectores
- Requerimientos para implementar y calibrar sistemas de bajo costo
- Diseñar e implementar, como trabajos practicos, dos metodos para la captura de objetos en 3D
- Identificar ideas para projectos que resulten en publicaciones

Triangulation and Scanning with Swept-Planes







Structured Lighting using Projector-Camera Systems









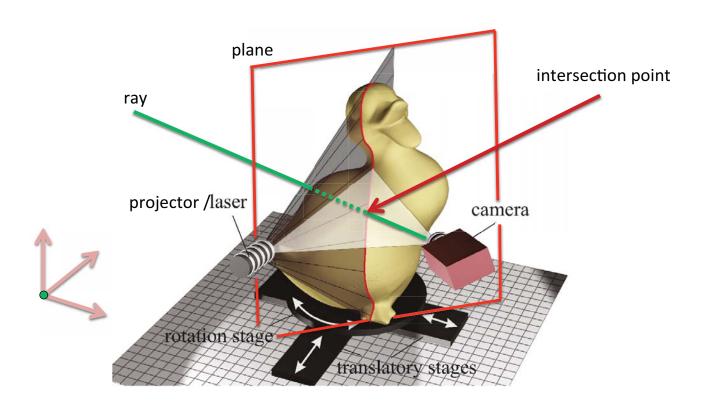
Que hace falta saber?

- Algebra Lineal
- Geometria Analítica en 3D
- Geometria Afin y Projectiva
- Estructuras de Datos / Complejidad
- Metodos Numericos
- Procesamiento de Imagenes
- Programacion en Matlab, C++ y/o Java
- Interes en construir y armar (DIY)

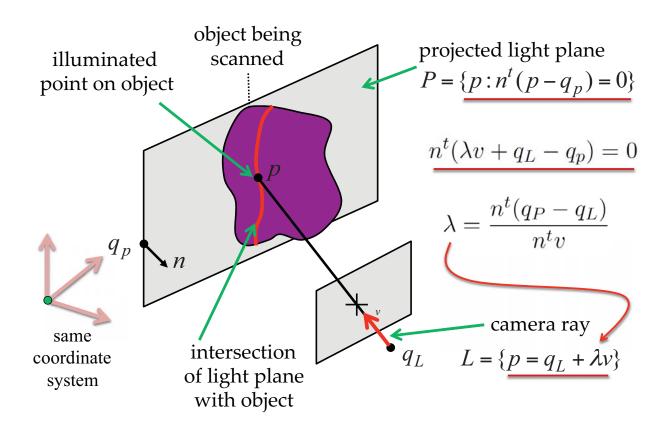
Plan del Curso

- 1. Introducción
- 2. Las Matemáticas de la Triangulación en 3D
- 3. 3D Scanning con Barrido de Planos
- 4. Calibración de Cameras y Fuentes de Luz
- 5. Superficies, Nubes de Puntos, Mallas Poligonales
- 6. Iluminación Estructurada
- 7. Calibración de Proyectores
- 8. Combinación de Múltiples Puntos de Vista
- 9. Reconstrucción de Superficies
- 10. Procesamiento de Geometria

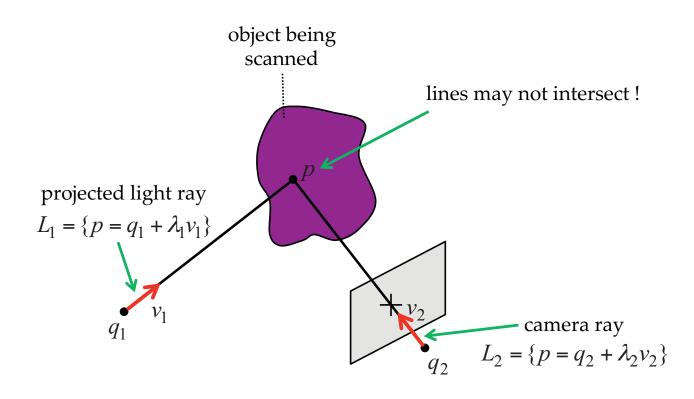
3D Triangulation: Ray-Plane Intersection



Triangulation by Line-Plane Intersection



Triangulation by Line-Line Intersection



Gray Code Structured Lighting

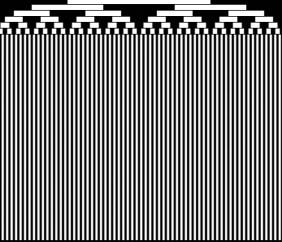


3D Reconstruction using Structured Light [Inokuchi 1984]

- Recover 3D depth for each pixel using ray-plane intersection
- Determine correspondence between camera pixels and projector planes by projecting a temporally-multiplexed binary image sequence
- Each image is a bit-plane of the Gray code for each projector row/column

Gray Code Structured Lighting





3D Reconstruction using Structured Light [Inokuchi 1984]

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- Determine correspondence between camera pixels and projector planes by projecting a temporally-multiplexed binary image sequence
- Each image is a bit-plane of the Gray code for each projector row/column
- Encoding algorithm: integer row/column index → binary code → Gray code

Projector-Camera Calibration

Brown University School of Engineering

Projector-Camera Calibration

http://mesh.brown.edu/calibration

Moreno Home

Taubin Home

Resources

- Paper
- Source code
- Software binary for Microsoft Windows
- MATLAB Projector Calibration [soon]
- Sample data
- Software manual
- Presentation
 slides

3DIMPVT 2012:

3D Imaging, Modeling, Processing, Visualization and Transmission

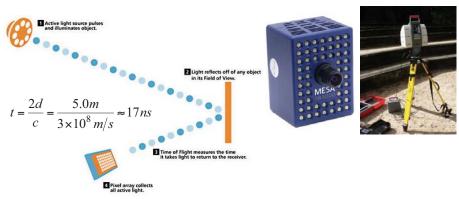
Simple, Accurate, and Robust Projector-Camera Calibration

Daniel Moreno and Gabriel Taubin

Abstract

Structured-light systems are simple and effective tools to acquire 3D models. Built with off-the-shelf components, a data projector and a camera, they are easy to deploy and compare in precision with expensive laser scanners. But such a high precision is only possible if camera and projector are both accurately calibrated. Robust calibration methods are well established for cameras but, while cameras and projectors can both be described with the same mathematical model, it is not clear how to adapt these methods to projectors. In consequence, many of the proposed projector calibration techniques make use of a simplified model, neglecting lens distortion, resulting in loss of precision. In this paper, we present a novel method to estimate the image coordinates of 3D points in the projector image plane. The method relies on an uncalibrated camera and makes use of local homographies to reach sub-pixel precision. As a result, any camera model can be used to describe the projector, including the extended pinhole model with radial and tangential distortion coefficients, or even those with more complex lens distortion models.

Time of Flight 3D Scanning



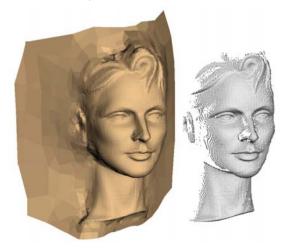


Single Shot Structured Lighting: MS Kinect



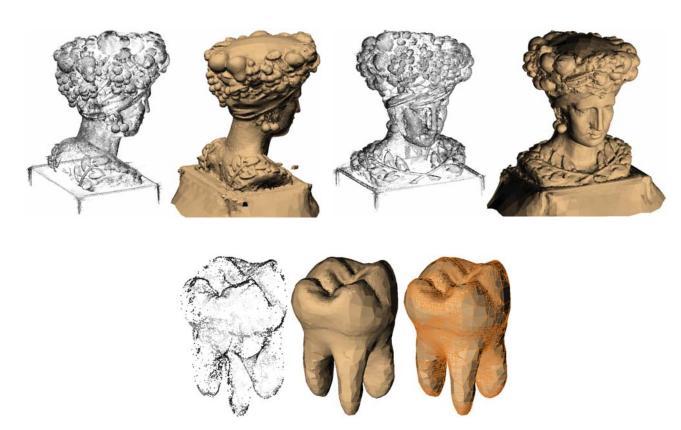
SSD: Smooth Signed Distance Surface Reconstruction F. Calakli, G. Taubin, Computer Graphics Forum, 2011.





- A new mathematical formulation
- And a particular algorithm
- To reconstruct a watertight surface
 From a static oriented point cloud

Particularly Good at Extrapolating Missing Data



Computer Graphics Forum, Vol. 30, No. 7, 2011 [Pacific Graphics 2011] Smooth Signed Distance Surface Reconstruction Fatil Calakli and Gabriel Taubin







lome

Paper

http://mesh.brown.edu/ssd

Software

Abstract

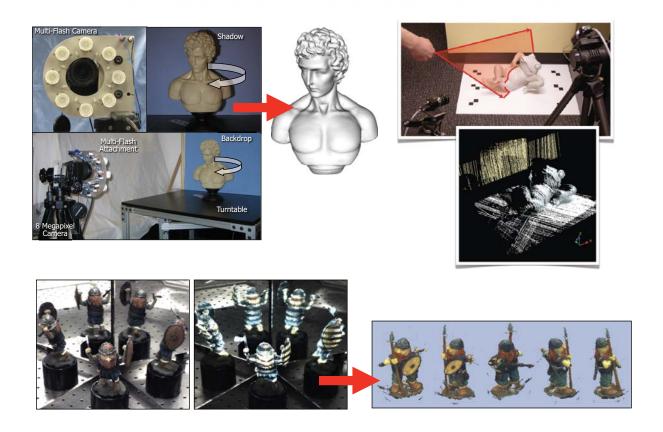
We introduce a new variational formulation for the problem of reconstructing a watertight surface defined by an implicit equation, from a finite set of oriented points; a problem which has attracted a lot of attention for more than two decades. As in the Poisson Surface Reconstruction approach, discretizations of the continuous formulation reduce to the solution of sparse linear systems of equations. But rather than forcing the implicit function to approximate the indicator function of the volume bounded by the implicit surface, in our formulation the implicit function is forced to be a smooth approximation of the signed distance function to the surface. Since an indicator function is discontinuous, its gradient does not exist exactly where it needs to be compared with the normal vector data. The smooth signed distance has approximate unit slope in the neighborhood of the data points. As a result, the normal vector data can be incorporated directly into the energy function without implicit function smoothing. In addition, rather than first extending the oriented points to a vector field within the bounding volume, and then approximating the vector field by a gradient field in the least squares sense, here the vector field is constrained to be the gradient of the implicit function, and a single variational problem is solved directly in one step. The formulation allows for a number of different efficient discretizations, reduces to a finite least squares problem for all linearly parameterized families of functions, and does not require boundary conditions. The resulting algorithms are significantly simpler and easier to implement, and produce results of quality comparable with state-of-the-art algorithms. An efficient implementation based on a primal-graph octree-based hybrid finite element-finite difference discretization, and the Dual Marching Cubes isosurface extraction algorithm, is shown to produce high quality crack-free adaptive manifold polygon meshes.

■ Acknowledgment of Support

The material presented in this web site describe work supported by the National Science Foundation under Grants No. CCF-0729126, IIS-0808718, and CCF-0915661.

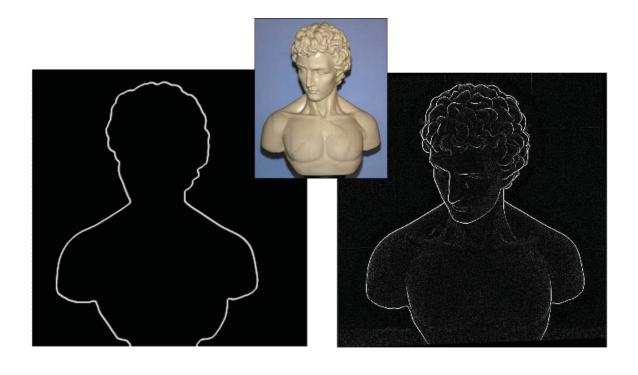
Final Projects which Resulted in Publications

Some Methods to Capture 3D Point Clouds



Beyond Silhouettes: Surface Reconstruction using Multi-Flash Photography

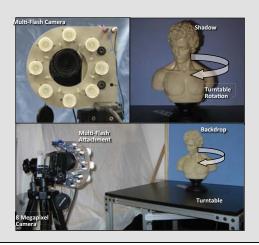
D. Crispell, D. Lanman, P. Sibley, Y. Zhao and G. Taubin [3DPVT 2006]



Multi-Flash 3D Photography: Capturing the Shape and Appearance of 3D Objects

A new approach for reconstructing 3D objects using shadows cast by depth discontinuities, as detected by a multi-flash camera. Unlike existing stereo vision algorithms, this method works *even with plain surfaces*, including unpainted ceramics and architecture.

Data Capture: A turntable and a digital camera are used to acquire data from 670 viewpoints. For each viewpoint, we capture a set of images using illumination from four different flashes. Future embodiments will include a small, inexpensive



Multi-Flash Turntable Sequence: Input Image

Estimated Shape: 3D Point Cloud

Recovered Appearance: Phong BRDF Model













Recovering a Smooth Surface

The reconstructed point cloud can possess errors, including gaps and noise. To minimize these effects, we find an implicit surface which interpolates the 3D points. This method can be applied to any 3D point cloud, including those generated by laser scanners.



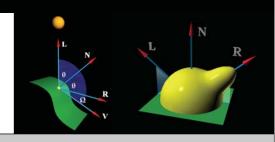
Multi-Flash 3D Photography: Photometric Reconstruction

Using the implicit surface, we can determine which points are visible from each viewpoint. To model the material properties of the surface, we fit a per-point Phong BRDF model to the set of visible reflectance observations (using a total of 67 viewpoints).



Diffuse

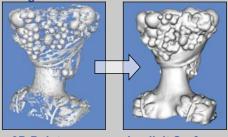
Specular







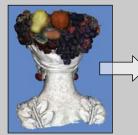
Multi-Flash Turntable Sequence



3D Point Implicit Surface Cloud



Phong Specular

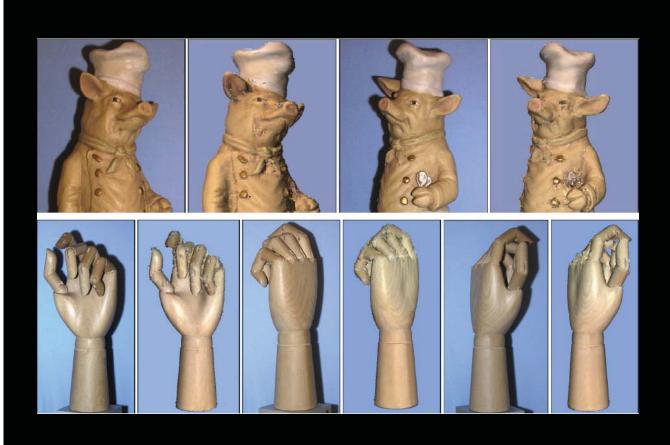


Phong (Diffuse)



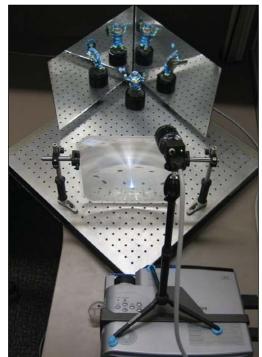
Estimated Phong Appearance Model





Surround Structured Lighting: 3-D Scanning with Orthographic Illumination

D. Lanman, D. Crispell, G. Taubin [CVIU 2009]

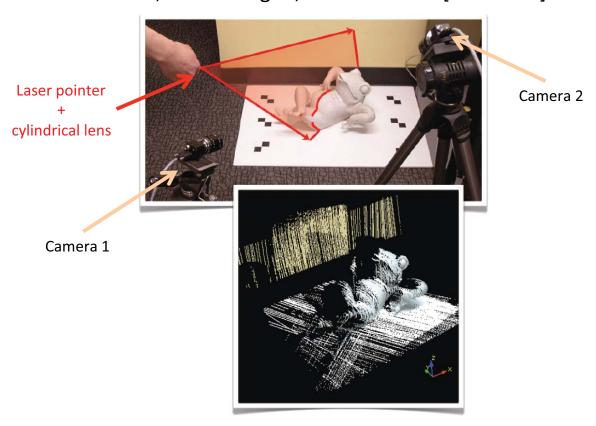




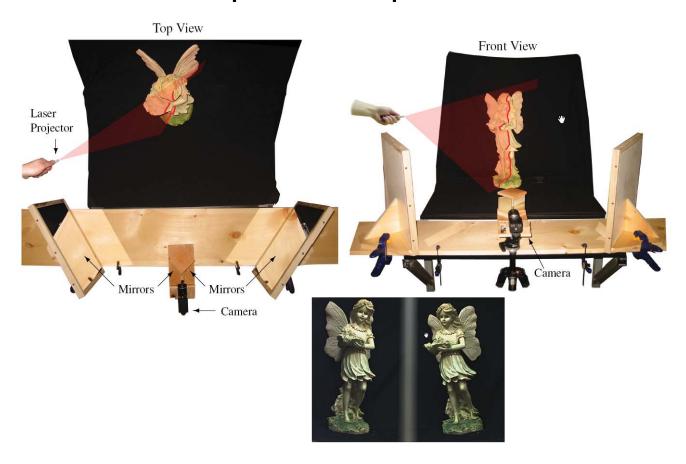


3D Slit Scanning with Planar Constraints

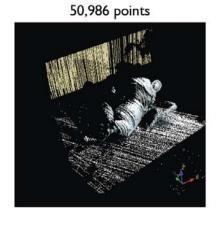
M. Leotta, A. Vandergon, and G. Taubin [CGF 2008]



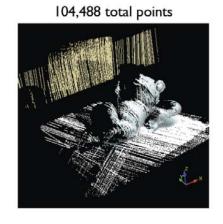
Catadioptric Stereo Implementation



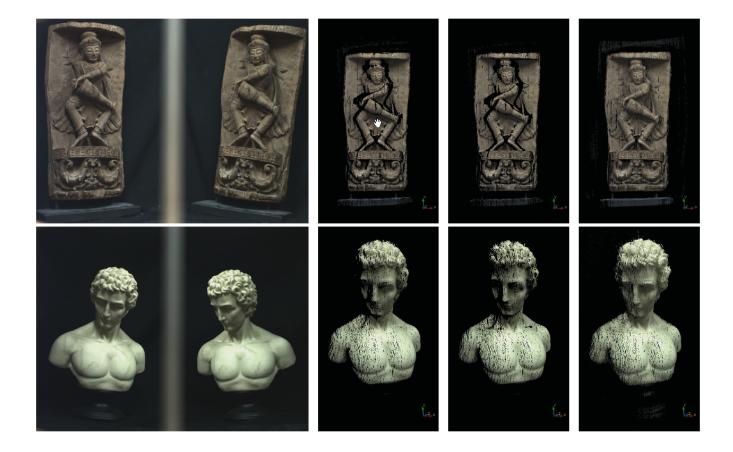
Can Estimate Points Visible From One Camera

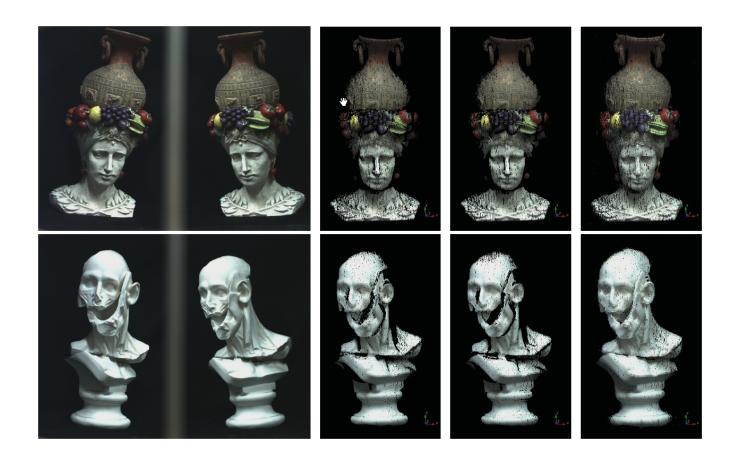












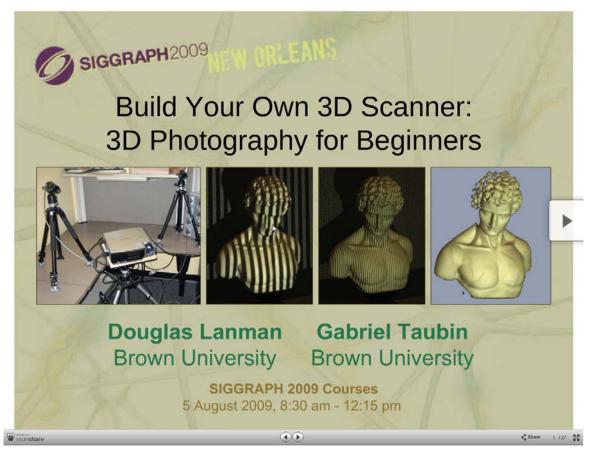
Schedule for this week and next

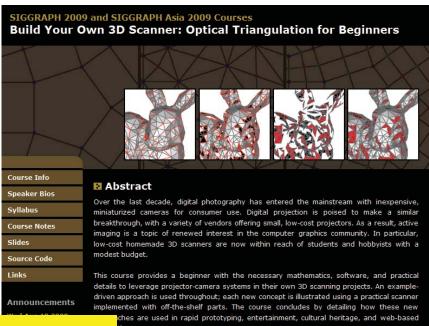
- Introduction to 3D Scanning
- The Mathematics of 3D Triangulation
- 3D Scanning with Swept-Planes | Slit scanner
- Camera and Swept-Plane Light Source Calibration

Lecture Notes and Additional Resources

- Download Course Notes from
- http://mesh.brown.edu/byo3d
- Or just Google search for BYO3D
- Courses on 3D Photography taught at Brown University
- http://mesh.brown.edu/3DP
- This Course
- http://mesh.brown.edu/3DP-FCEN-2013

http://mesh.brown.edu/byo3d/





http://mesh.brown.edu/byo3d

erequisites

oom 511.

Tues July 17 2009:

See this course at SIGGRAPH 2009 on Wed August 5 from 8:30 AM - 12:15 PM in

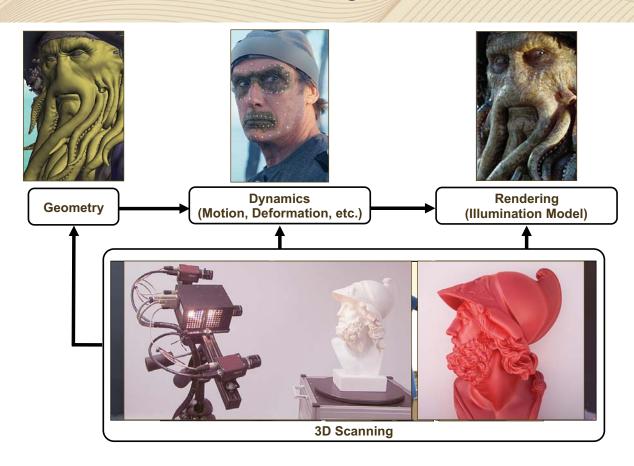
More Info...

Attendees should have a basic undergraduate-level knowledge of linear algebra. While executables are provided for beginners, attendees with prior knowledge of Matlab, C/C++, and Java programming will be able to directly examine and modify the provided source code.

■ About this Website

This website serves as an addendum to the course material. Updated versions of the course notes, slides, and source code are distributed here. In addition, links to recent do-it-yourself projects in 3D scanning, as well as late-breaking academic works, are maintained. We encourage course attendees to contact the organizers so we can post links to your own projects, as well as hear your feedback about how the course could be improved.

Introduction to 3D Scanning



Applications of 3D Scanning: Entertainment and Consumer Applications



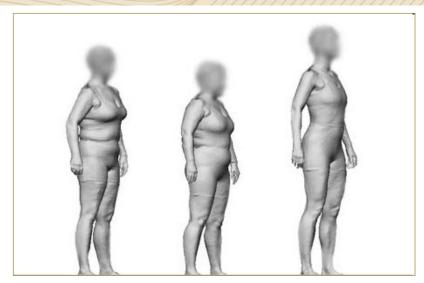


- Import sculptures into a 3D modeling/rendering pipeline
- Capture geometric (and photometric) properties for relighting
- Fit clothes, track 3D interaction, free-viewpoint video (3D TV), etc.

Andreas Wenger et al. Performance Relighting and Reflectance Transformation with Time-Multiplexed Illumination. ACM SIGGRAPH, 2005

Applications of 3D Scanning: Entertainment and Consumer Applications





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Andreas Wenger Mt. aWaserhöuselmet Ale Bydalliallyle 60 Rédlectafi Dey Taanisf Screation with Time-Multiple West Wisnaih 6 to on put 6 M25 ICS GRAPH, 2005

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Applications of 3D Scanning: Historical Preservation

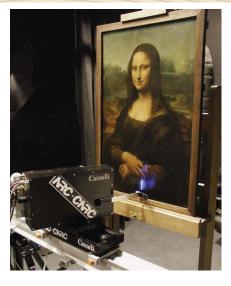




- Preserve/restore deteriorating works and unite dispersed collections
- Facilitate academic study (tooling, lighting, pentimenti, revision history)
- Replicate collections (souvenirs, retain repatriated works, etc.)

M. Levoy et al. The Digital Michelangelo Project: 3D Scanning of Large Statues. ACM SIGGRAPH, 2000

Applications of 3D Scanning: Historical Preservation





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P. Debevec. Making "The Parthenon". Intl. Sym. on Virtual Reality, Archaeology, and Cultural Heritage, 2005

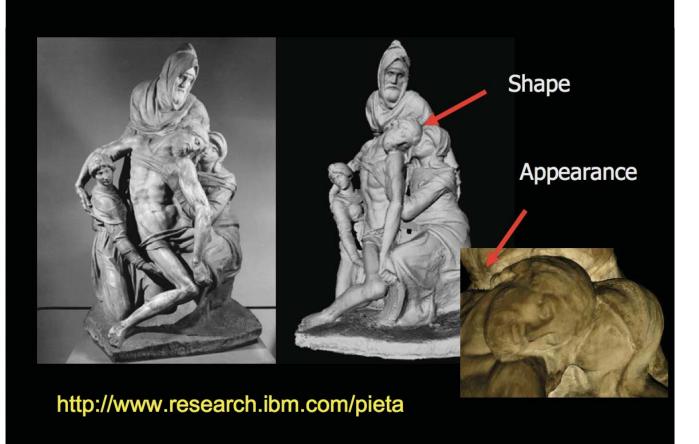
Applications of 3D Scanning: Historical Preservation





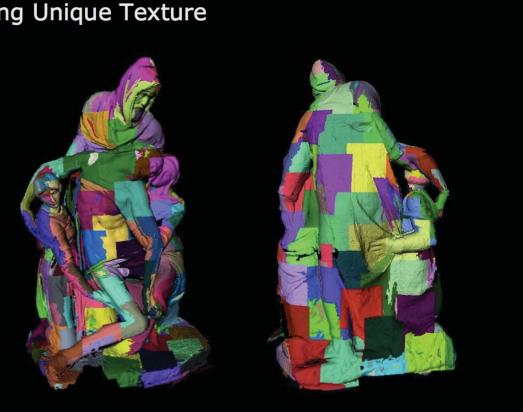
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IBM Pietà 3D Scanning Project: 1998-2000

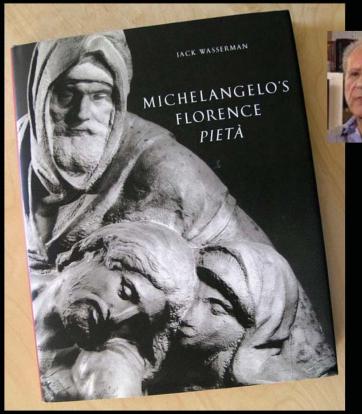


Pieta` Project

Remapping Unique Texture



Wasserman's Pietà Book



Princeton University Press 2003

Capturing ~800 scans (1998)







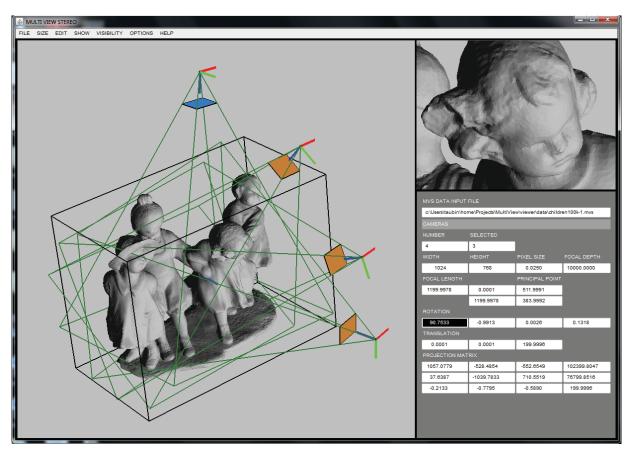




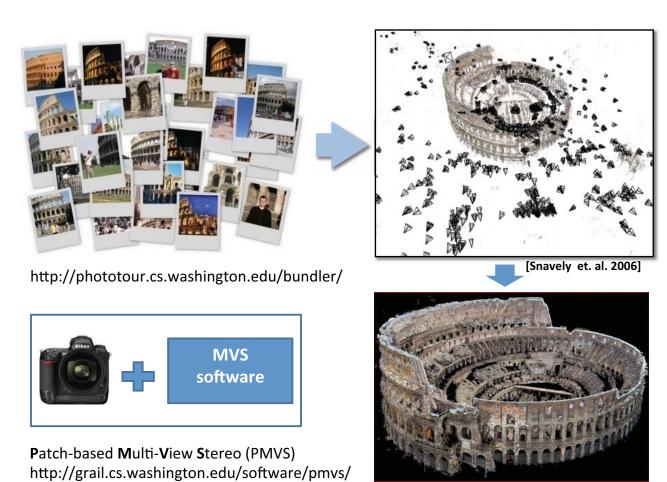




Surface Reconstruction from Multi-View Data







[Furukawa and Ponce 2008]



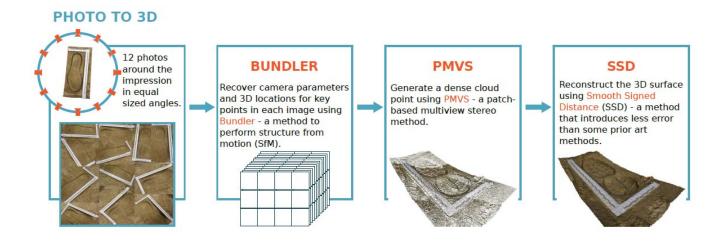
Fig. 1 Reconstruction of the side of a castle model: The input point cloud (top-left), Surface reconstructed by the proposed algorithm(top-right), Two views from the surface and color map reconstructed by the proposed algorithm (bottom).



Fig. 6 Reconstruction of a brick with cuneiform, Mesopotamian, 859-840 BCE, clay, Overall 35 x 35 x 11 cm, Williams College Museum of Art, Williamstown, MA, Gift of Professor Edgar J. Banks and Dr. John Henry Haynes, Class of 1876,(20.1.33.A). Top row: the input point cloud (left), and surface geometry (right) reconstructed by the proposed algorithm. Middle row: Two views from surface and color map reconstructed by the proposed algorithm. Bottom row: 6 examples from the set of 21 images that are used for shape acquisition.

Accurate 3D Footwear Impression Recovery From Photographs,

F. A. Andalo, F. Calakli, G. Taubin, and S. Goldenstein, International Conference on Imaging for Crime Detection and Prevention (ICDP-2011).



Comparable to 3D Laser Scanner





EXPERIMENTAL RESULTS





- d_q: Haursdoff distance map between the scanned
- shoe print and the scanned shoe sole.

 d_m: Haursdoff distance map between our 3D model and the scanned shoe sole.

Shoeprint #	$\overline{d_g}$	$\overline{d_m}$	$\overline{d_m} - \overline{d_g}$
1	9.996	10.002	0.006
2	8.157	8.660	0.503
3	8.715	9.480	0.765
4	8.816	9.114	0.298

(mm)

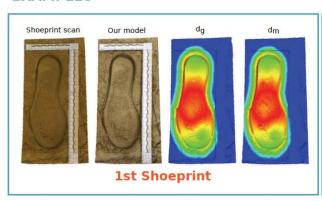
CONCLUSIONS

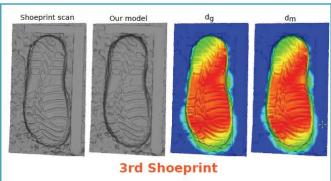
We presented a pipeline to recover footwear impressions from crime scenes using multiview stereo, which has not been considered for this kind of application until now.

Despite the simplicity, the obtained surfaces are comparable with 3D scanning.

Future work: more experiments -number of images, angle between images, comparison with casting.

EXAMPLES





Applications of 3D Scanning: Medical Imaging and Surgical Planning



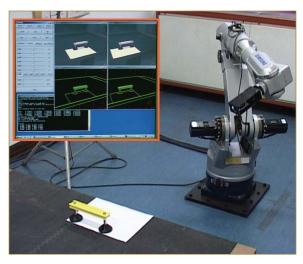
- Medical imaging (X-ray, CT, MRI, etc.) and surgical planning
- Measuring dimensions (dental impressions and hip replacement surgery)
- Tele-surgery (augmented virtual reality, video see-through, etc.)

Applications of 3D Scanning: Medical Imaging and Surgical Planning



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Applications of 3D Scanning: Robotics (Interaction and Navigation)







- Motion planning (manipulation, gripping, pushing/pulling, etc.)
- Simultaneous localization and mapping (SLAM)
- Autonomous navigation (DARPA Grand/Urban Challenge)

Applications of 3D Scanning: Robotics (Interaction and Navigation)

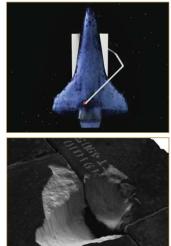




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Applications of 3D Scanning: Inspection and Reverse Engineering



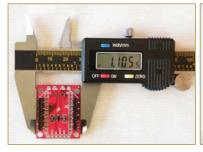




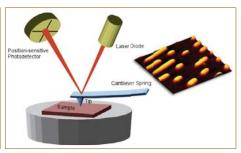
- Manufacturing and process control (tolerances and alignment)
- Reverse engineering (repairing antiques and replicating designs)
- Remote inspection (inaccessible or dangerous environments)

Taxonomy of 3D Scanning: Direct Contact









Contact — Direct Measurements (rulers, calipers, pantographs, coordinate measuring machines (CMM), AFM)

Non-Contact

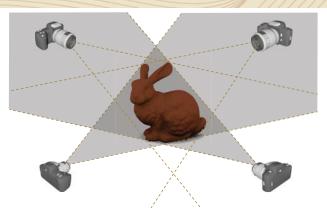
Real-Time High-Definition Stereo on GPGPU using Progressive Multi-Resolution Adaptive Windows Y. Zhao, and G. Taubin, Image and Vision Computing 2011.



Taxonomy of 3D Scanning: Stereo/Multi-view Photography



Taxonomy of 3D Scanning: Shape-from-Silhouettes



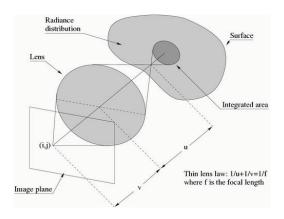


Taxonomy of 3D Scanning: Shape-from-Silhouettes





Taxonomy of 3D Scanning: Shape-from-Focus/Defocus

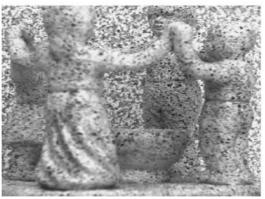




M. Watanabe and S. Nayar. Rational filters for passive depth from defocus. *Intl. J. of Comp. Vision*, 27(3):203-225, 1998

Taxonomy of 3D Scanning: Shape-from-Focus/Defocus

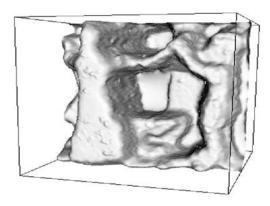






Taxonomy of 3D Scanning: Shape-from-Focus/Defocus

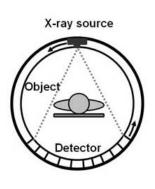


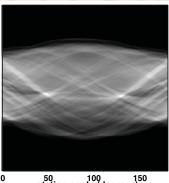


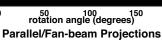


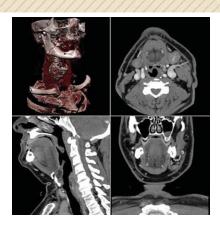
M. Watanabe and S. Nayar. Rational filters for passive depth from defocus. *Intl. J. of Comp. Vision*, 27(3):203-225, 1998

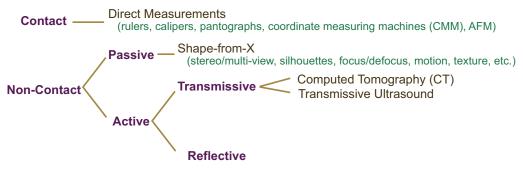
Taxonomy of 3D Scanning: Computed Tomography (CT)











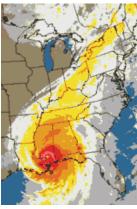
Taxonomy of 3D Scanning: Non-optical Active Methods



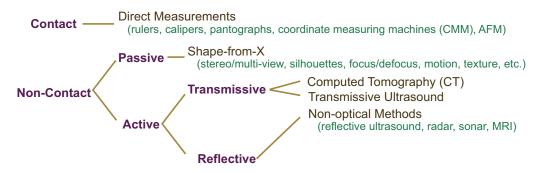












Taxonomy of 3D Scanning: Active Variants of Passive Methods









Contact

Direct Measurements
(rulers, calipers, pantographs, coordinate measuring machines (CMM), AFM)

Passive

Shape-from-X
(stereo/multi-view, silhouettes, focus/defocus, motion, texture, etc.)

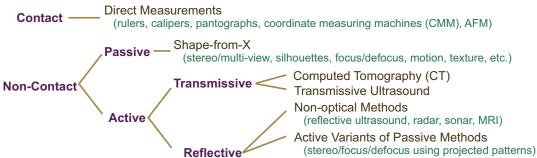
Computed Tomography (CT)
Transmissive Ultrasound

Non-optical Methods
(reflective ultrasound, radar, sonar, MRI)

Active Variants of Passive Methods
(stereo/focus/defocus using projected patterns)

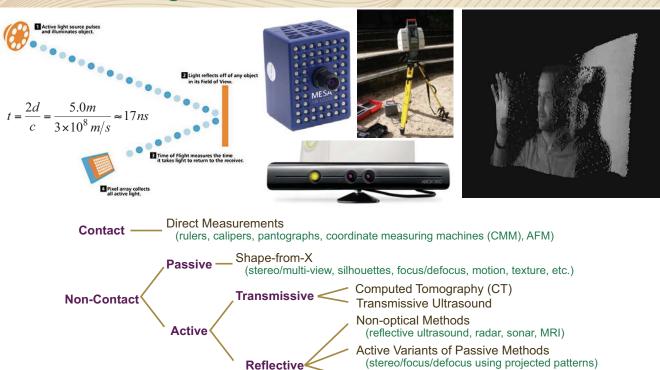
Taxonomy of 3D Scanning: Active Variants of Passive Methods





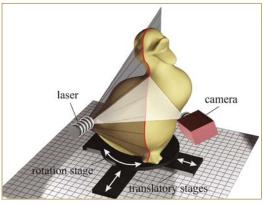
M. Watanabe and S. Nayar. Rational Filters for Passive Depth from Defocus. *Intl. J. of Comp. Vision*, 27(3):203-225, 1998

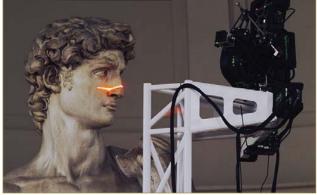
Taxonomy of 3D Scanning: Time-of-Flight

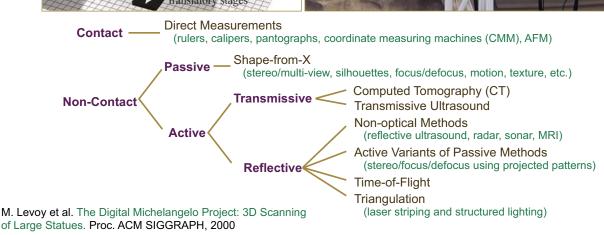


Time-of-Flight

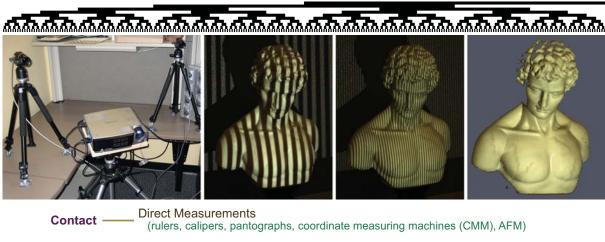
Taxonomy of 3D Scanning: Triangulation with Laser Striping

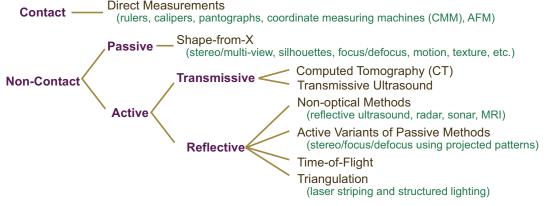




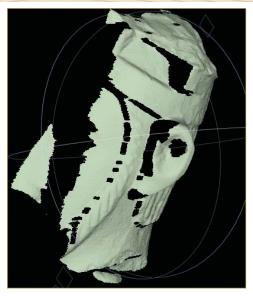


Taxonomy of 3D Scanning: Triangulation with Structured Lighting





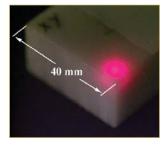
Challenges of Optical 3D Scanning

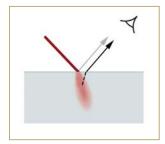


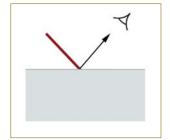


- Must be simultaneously illuminated and imaged (occlusion problems)
- Non-Lambertian BRDFs (transparency, reflections, subsurface scattering)
- Acquisition time (dynamic scenes), large (or small) features, etc.

Challenges of Optical 3D Scanning



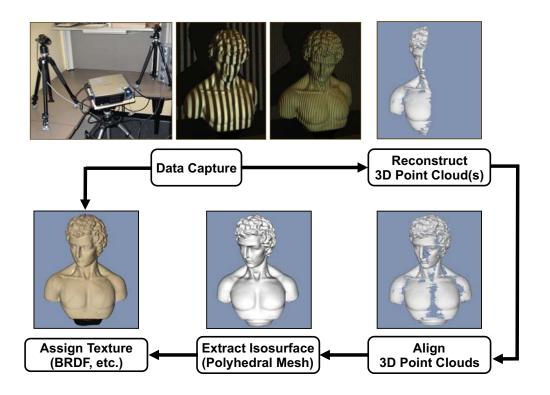




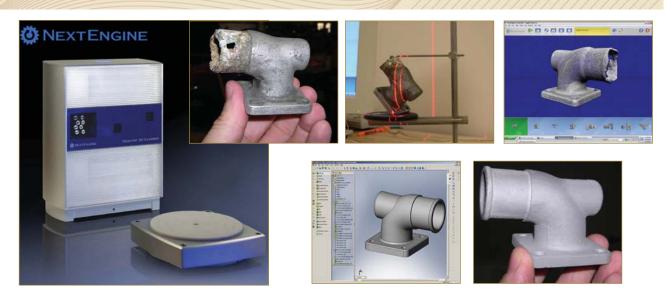


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The 3D Scanning Pipeline



Commercial 3D Scanners



Features, Limitations, and Benefits

- Most commercial scanners use laser striping + turntables/fiducials
- Cost varies (NextEngine ~\$3,000 USD, others more expensive)
- Complete pipeline (including registration and isosurface extraction)

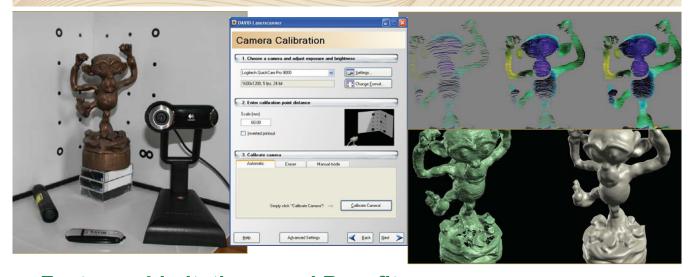
Commercial 3D Scanners



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Do-It-Yourself (DIY) 3D Scanners



Features, Limitations, and Benefits

- Most DIY scanners also use laser striping + turntables
- Relatively inexpensive (DAVID laser scanner ~\$550 USD for starter kit)
- Incomplete pipeline (lacking registration and isosurface extraction)
- Most (but not all) lack proper camera and light source calibration

Do-It-Yourself (DIY) 3D Scanners





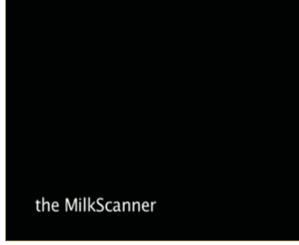


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Topics/Scanners in this Course

1) Scanning with Swept-Planes







2) Structured Lighting using Projector-Camera Systems









3) Post-processing Pipeline: Registration and Isosurfaces

When not to Scan?



- Scanning is (usually) unnecessary when output is another image!
- Better to use image-based rendering (light fields, QTVR, etc.)

Marc Levoy. Stanford Spherical Gantry. On-line, 2005

Next Class

- Introduction to 3D Scanning
- The Mathematics of 3D Triangulation
- 3D Scanning with Swept-Planes | Slit scanner
- Camera and Swept-Plane Light Source Calibration

Introducción a la Fotografia 3D UBA/FCEN Marzo 27 – Abril 12 2013 Clase 2 : Miercoles Abril 3

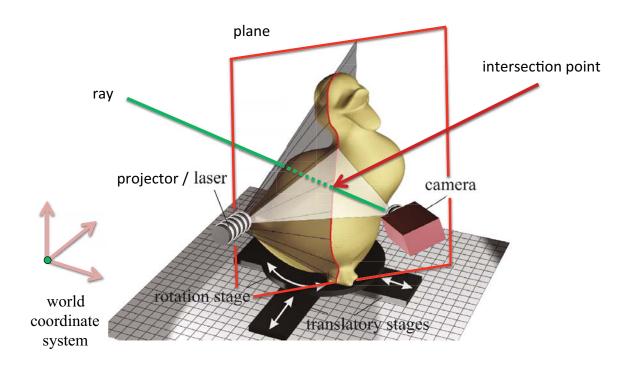
Gabriel Taubin
Brown University



Las matemáticas de la triangulacion 3D

- Triangulation por interseccion de linea y plano
- Triangulation por interseccion de linea y linea
- Puntos, vectores, lineas, rayos, and planos
- Que es una camara?
- Que es una image?
- •

3D triangulation: ray-plane Intersection





What is a Camera?

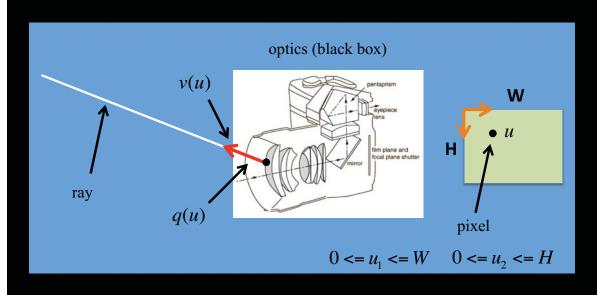


What is a Camera?

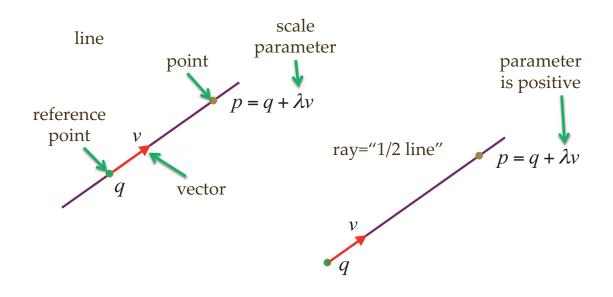


Modelo Geometrico General de una Camara

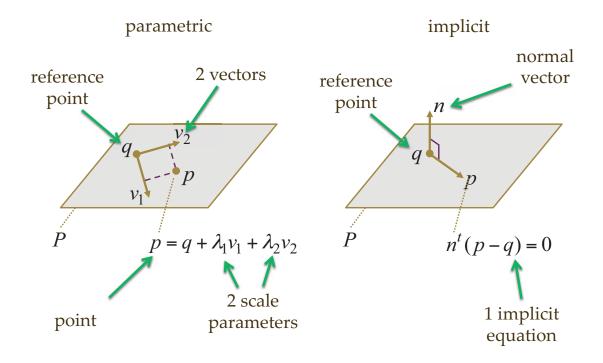
- Funcion que a cada punto de la imagen le hace corresponder un rayo
- El dominio esta contenido en un rectangulo y la funcion es continua
- En muchos casos el análisis es mas simple en el espacio de los rayos



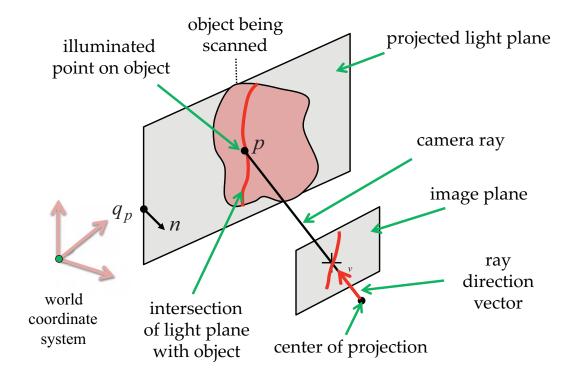
Representation of Lines and Rays



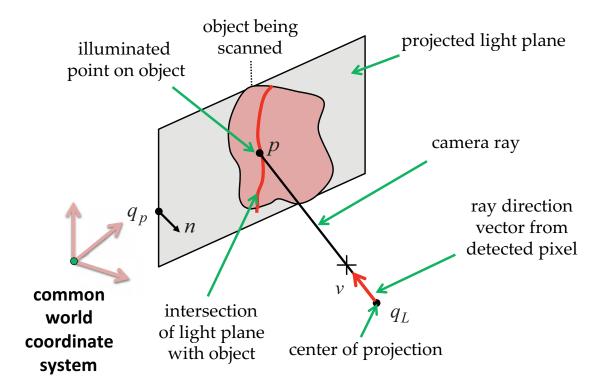
Representation of Planes



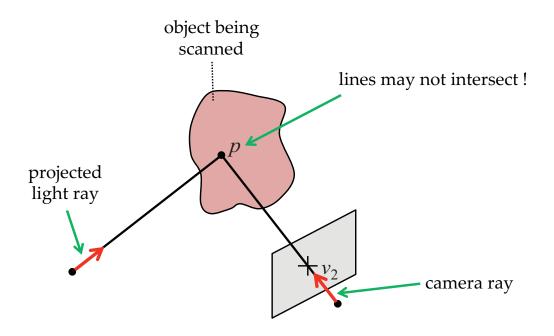
3D Triangulation by Line-Plane intersection



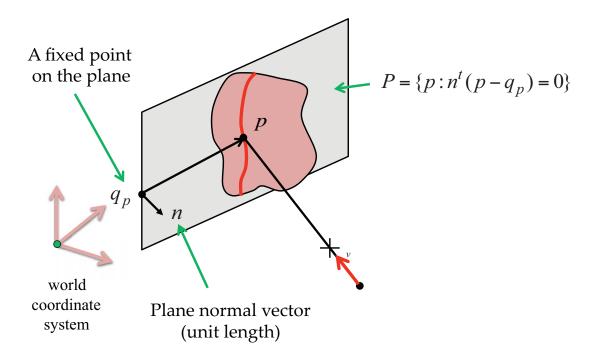
If camera and projector are calibrated



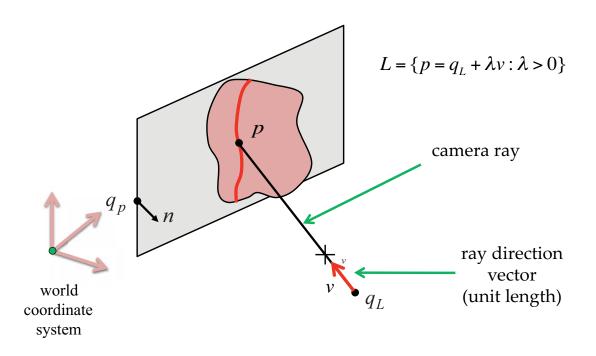
3D Triangulation by Line-Line Intersection



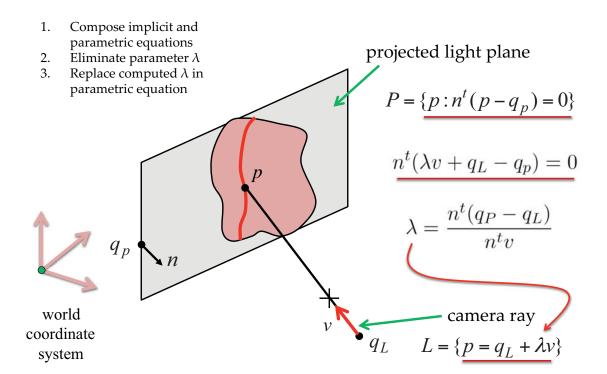
Implicit equation of the plane



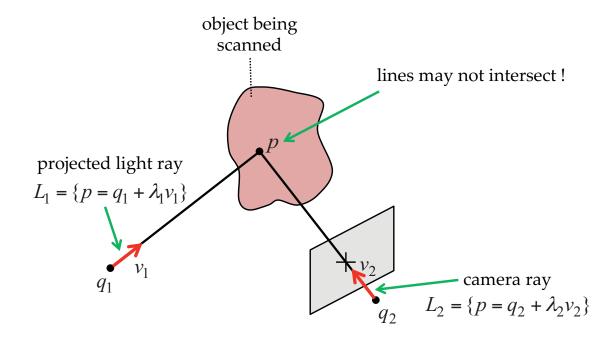
Parametric equation of the ray



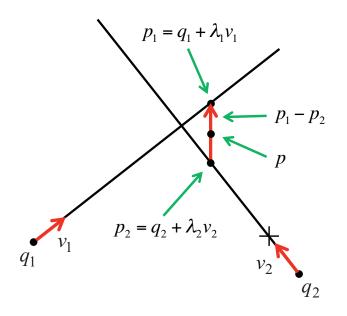
Triangulation by Line-Plane Intersection



Triangulation by Line-Line Intersection



Triangulation by Line-Line Intersection



$$L_{1} = \{p_{1} = q_{1} + \lambda_{1}v_{1}\}$$

$$L_{2} = \{p_{2} = q_{2} + \lambda_{2}v_{2}\}$$

Minimize

$$E(\lambda_1, \lambda_2) = dist(p_2 - p_1)^2$$

Necessary conditions

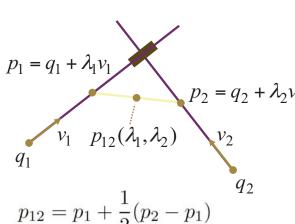
$$v_1^t(p_1 - p_2) = 0$$

$$v_2^t(p_2 - p_1) = 0$$

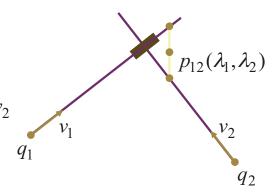
$$p = (p_1 + p_2)/2$$

Approximate Line-Line Intersection

Midpoint of segment joining arbitrary points in the two lines



Least-squares approach



Find parameters which minimize

$$||(q_2 + \lambda_2 v_2) - (q_1 + \lambda_1 v_1)||^2$$

Approximate Line-Line Intersection

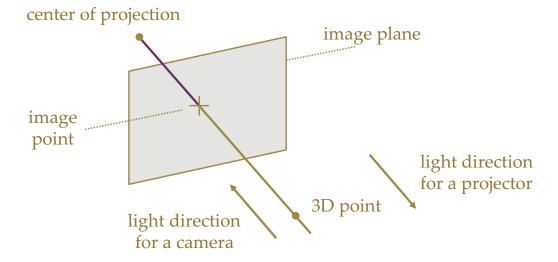
$$p_{12} = p_1 + \frac{1}{2}(p_2 - p_1)$$

$$p_1 = q_1 + \lambda_1 v_1$$

$$p_2 = q_2 + \lambda_2 v_2$$

$$\begin{pmatrix} \lambda_1 \\ \lambda_2 \end{pmatrix} = \begin{pmatrix} \|v_1\|^2 & -v_1^t v_2 \\ -v_2^t v_1 & \|v_2\|^2 \end{pmatrix}^{-1} \begin{pmatrix} v_1^t (q_2 - q_1) \\ v_2^t (q_1 - q_2) \end{pmatrix}$$

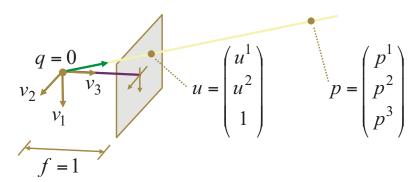
Perspective Projection (Pinhole Model)



Calibration: mapping from image points to rays

The Ideal Pinhole Camera

camera coordinate system = world coordinate system

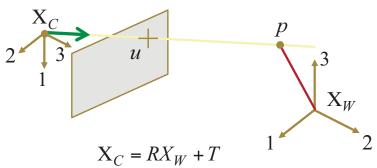


$$\begin{pmatrix} p^1 \\ p^2 \\ p^3 \end{pmatrix} = \lambda \left[v_1 | v_2 | q \right] \begin{pmatrix} u^1 \\ u^2 \\ 1 \end{pmatrix} \qquad \left[v_1 | v_2 | q \right] = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

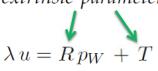
The General Pinhole Model

camera coordinate system

world coordinate system



extrinsic parameters



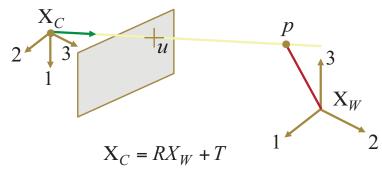
Ideal assumptions

- Image lengths = world lengths
- Focal length = 1
- Image origin = optical center
- Image plane spanned by two basis vectors

The General Pinhole Model

camera coordinate system

world coordinate system



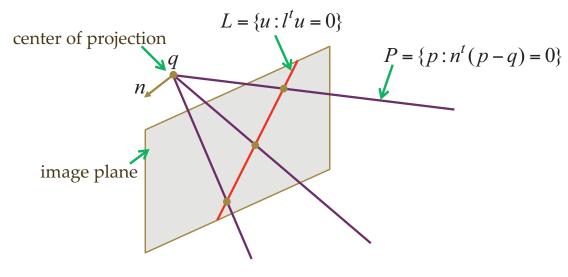
$$\lambda u = K(R p_W + T)$$

intrinsic parameters
$$K = \begin{pmatrix} f s_1 & f s_\theta & o^1 \\ 0 & f s_2 & o^2 \\ 0 & 0 & 1 \end{pmatrix}$$

$$\lambda u = K(R p_W + T)$$

Plane Defined by Image Line and Projection Center

Implicit equation of line in image coordinates



$$0 = \lambda l^t u = l^t (R p_W + T) = (R^t l)^t (p_W - (-R^t T)).$$

Desktop 3D Photography







Structured Lighting

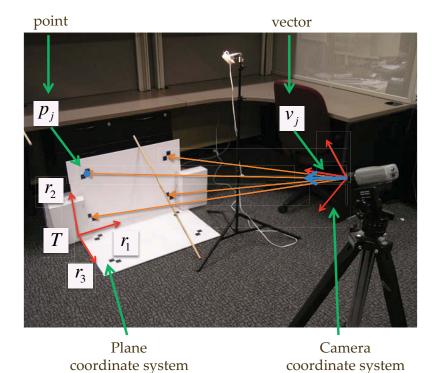








Estimating the equation of a plane



Given

$$\lambda_{j}v_{j} = Rp_{j} + T$$
$$j = 1,...,N$$

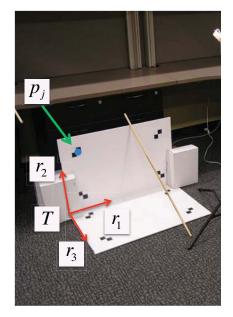
We want to estimate the rotation R and the translation T

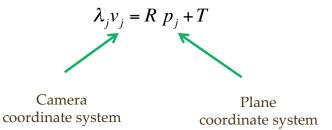
$$R = \left[r_1 r_2 r_3 \right]$$

How to solve this problem?

What is the minimum number of points necessary to solve the problem?

Estimating the equation of a plane





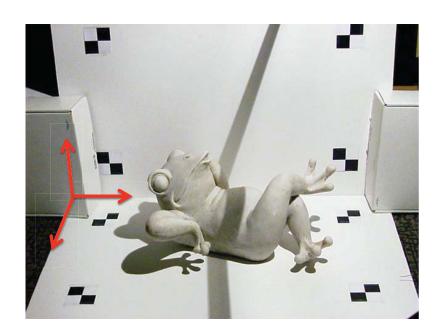
Implicit equation of plane in the camera coordinate system

$${q:r_3^t(q-T)=0}$$

Parametric equation of plane in the camera coordinate system

$${q = T + x r_1 + y r_2 + 0 r_3}$$
 $p = [x, y, 0]^t$

Estimating the equation of two planes

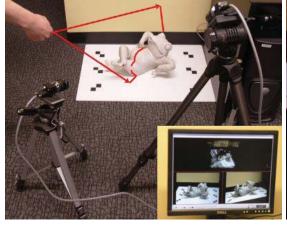


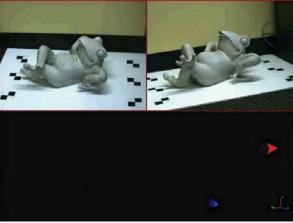
Introducción a la Fotografia 3D UBA/FCEN Marzo 27 – Abril 12 2013 Clase 3 : Jueves Abril 4

Gabriel Taubin
Brown University



Triangulation by Laser Striping





- Manually or mechanically translated laser stripe
- Per-pixel depth by ray-plane triangulation
- Requires accurate camera and laser plane calibration
- Popular solution for commercial and DIY 3D scanners

3D Photography on Your Desk: Bouguet and Perona [ICCV 1998]



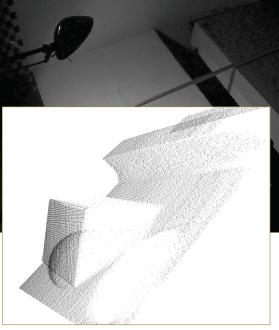


- DIY scanner using only a camera, a halogen lamp, and a stick
- Per-pixel depth by ray-plane triangulation
- Requires accurate camera and shadow plane calibration

J.-Y. Bouguet and P. Perona. 3D photography on your desk. *Intl. Conf. Comp. Vision*, 1998

3D Photography on Your Desk: Bouguet and Perona [ICCV 1998]





Assembling Your Own Scanner



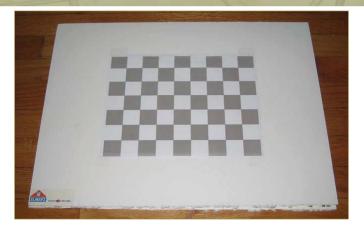
- Parts: camera (QuickCam 9000), lamp, stick, two planar objects [~\$100]
- Step 1: Build the calibration boards (include fiducials and chessboard)
- Step 2: Build the point light source (remove reflector and place in scene)
- Step 3: Arrange the camera, light source, and calibration boards

Assembling Your Own Scanner



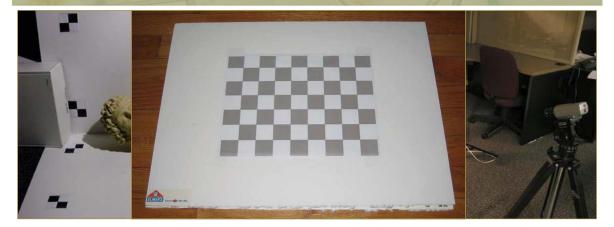
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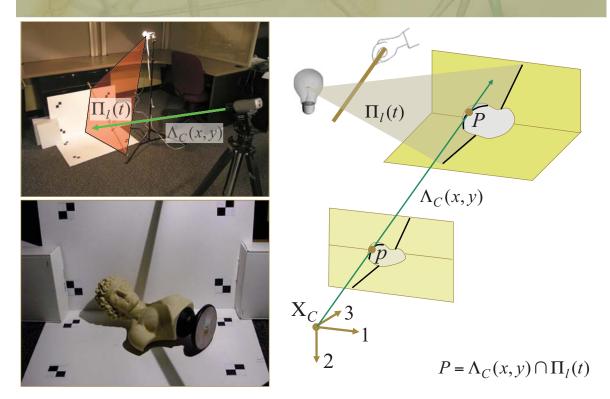
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Swept-Plane Reconstruction Geometry



Demo: Data Capture



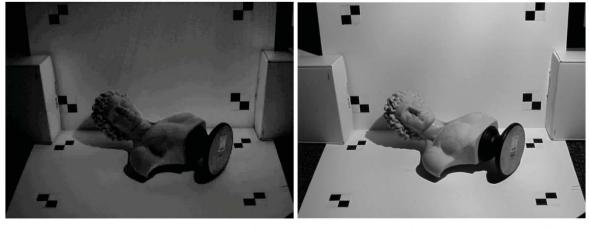
Video Processing: Assigning Per-Pixel Shadow Thresholds



 $I_{min}(x;y) = \min_{t} I(x;y;t)$

- Convert from RGB to grayscale (for luminance-domain processing)
- Determine per-pixel minimum and maximum value over sequence

Video Processing: Assigning Per-Pixel Shadow Thresholds

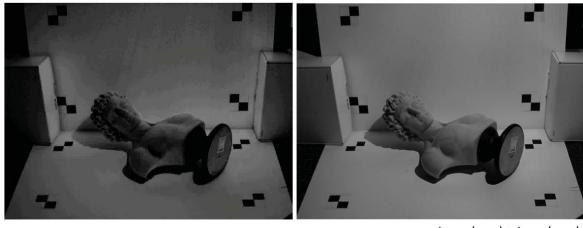


$$I_{min}(x;y) = \min_{t} I(x;y;t)$$

$$I_{max}(x;y) = \max_{t} I(x;y;t)$$

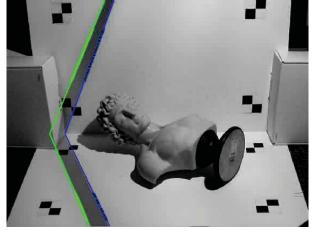
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- Determine per-pixel minimum and maximum value over sequence

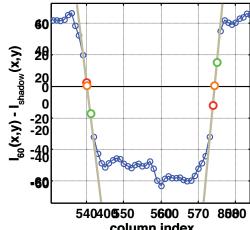
Video Processing: Assigning Per-Pixel Shadow Thresholds



- $I_{min}(x;y) = \min_{t} I(x;y;t)$
- $I_{shadow}(x;y) = \frac{I_{max}(x;y) + I_{min}(x;y)}{2}$
- Convert from RGB to grayscale (for luminance-domain processing)
- Determine per-pixel minimum and maximum value over sequence
- Evaluate per-pixel "shadow threshold" as average of min. and max.

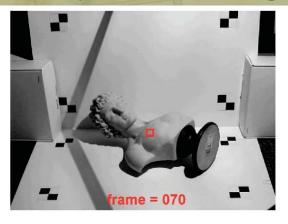
Video Processing: Spatial Shadow Edge Localization

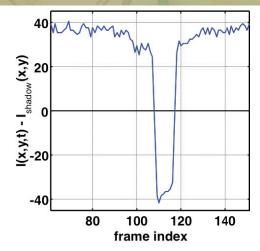




- Select region of interest on each calibration plane (occlusion-free)
- Estimate zero-crossings to find leading and trailing shadow boundaries
- Fit a line to the set of points along each shadow boundary
- → Result: Best-fit 2D lines for each shadow edge (in image coordinates)

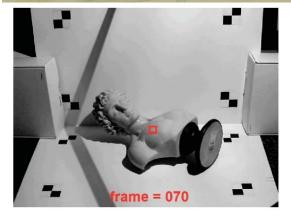
Video Processing: Temporal Shadow Edge Localization

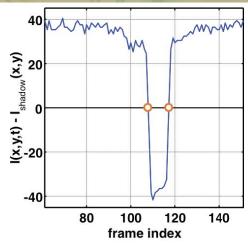




Tabulate per-pixel temporal sequence (minus shadow threshold)

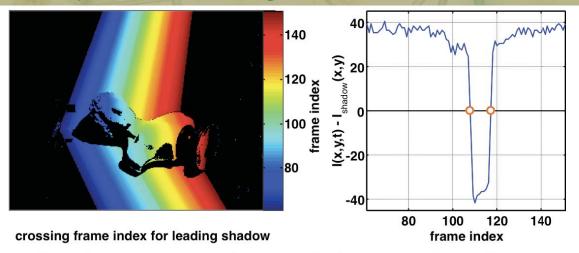
Video Processing: Temporal Shadow Edge Localization



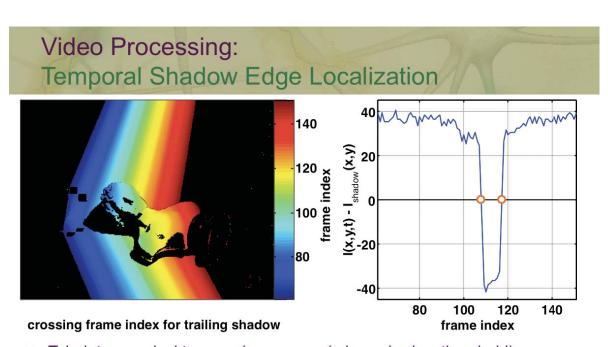


- Tabulate per-pixel temporal sequence (minus shadow threshold)
- Estimate zero-crossings to find shadow-crossing times

Video Processing: Temporal Shadow Edge Localization

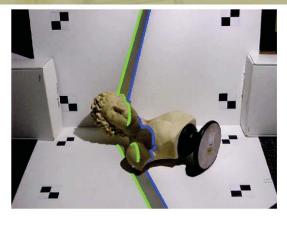


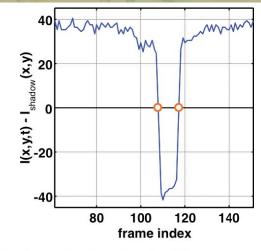
- Tabulate per-pixel temporal sequence (minus shadow threshold)
- Estimate zero-crossings to find shadow-crossing times



- Tabulate per-pixel temporal sequence (minus shadow threshold)
- Estimate zero-crossings to find shadow-crossing times

Video Processing: Temporal Shadow Edge Localization





- Tabulate per-pixel temporal sequence (minus shadow threshold)
- Estimate zero-crossings to find shadow-crossing times
- → Result: Use shadow-crossing time to lookup corresponding 3D plane

Course Schedule

- Introduction
- The Mathematics of 3D Triangulation
- 3D Scanning with Swept-Planes
- > Camera and Swept-Plane Light Source Calibration
- Reconstruction and Visualization using Point Clouds

Introducción a la Fotografia 3D UBA/FCEN Marzo 27 – Abril 12 2013 Clase 4 : Viernes Abril 5

Gabriel Taubin
Brown University



Course Schedule

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Modeling Lens Distortion





Cheap CMOS chip Cheap lens Cheap glue Cheap camera



Without lens distortion distortion

$$\begin{bmatrix} x_p \\ y_p \end{bmatrix} = \begin{bmatrix} f_x X^W / Z^W + c_x \\ f_y X^W / Z^W + c_y \end{bmatrix}$$

G. Bradski and A. Kaehler. Learning OpenCV. O' Reilly Media, 2008

Modeling Lens Distortion





Radial distortion

$$x_{\text{corrected}} = x(1 + k_1 r^2 + k_2 r^4 + k_3 r^6)$$

$$y_{\text{corrected}} = y(1 + k_1 r^2 + k_2 r^4 + k_3 r^6)$$

Modeling Lens Distortion





Tangencial distortion

$$x_{\text{corrected}} = x + [2p_1y + p_2(r^2 + 2x^2)]$$

$$y_{\text{corrected}} = y + [p_1(r^2 + 2y^2) + 2p_2x]$$

G. Bradski and A. Kaehler. Learning OpenCV. O' Reilly Media, 2008

Modeling Lens Distortion



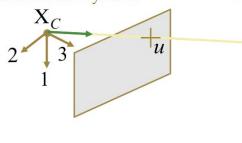


$$\begin{bmatrix} x_p \\ y_p \end{bmatrix} = (1 + k_1 r^2 + k_2 r^4 + k_3 r^6) \begin{bmatrix} x_d \\ y_d \end{bmatrix} + \begin{bmatrix} 2p_1 x_d y_d + p_2 (r^2 + 2x_d^2) \\ p_1 (r^2 + 2y_d^2) + 2p_2 x_d y_d \end{bmatrix}$$

Intrinsic Camera Calibration

camera coordinate system

world coordinate system



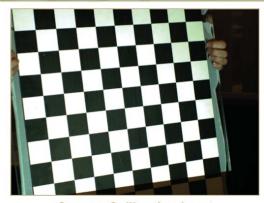
$$\lambda u = K(R p_W + T)$$

ovtrincia naramatara

intrinsic parameters

How to estimate intrinsic parameters and distortion model?
 (unknowns: focal length, skew, scale, principal point, and distortion coeffs.)

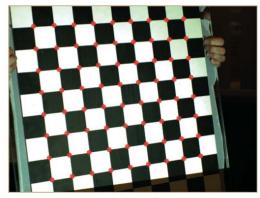
Intrinsic Camera Calibration



Camera Calibration Input

- How to estimate intrinsic parameters and distortion model?
 (unknowns: focal length, skew, scale, principal point, and distortion coeffs.)
- Popular solution: Observe a known calibration object (Zhang [2000])

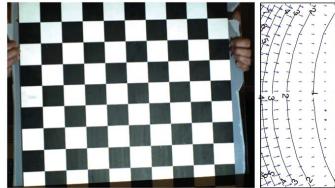
Intrinsic Camera Calibration



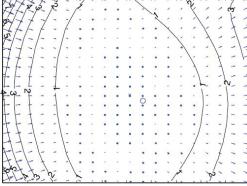
Camera Calibration Input

- How to estimate intrinsic parameters and distortion model?
 (unknowns: focal length, skew, scale, principal point, and distortion coeffs.)
- Popular solution: Observe a known calibration object (Zhang [2000])
- Each 2D chessboard corner yields two constraints on the 6-11 unknowns

Intrinsic Camera Calibration



Camera Calibration Input



Estimated Camera Lens Distortion Map

- How to estimate intrinsic parameters and distortion model?
 (unknowns: focal length, skew, scale, principal point, and distortion coeffs.)
- Popular solution: Observe a known calibration object (Zhang [2000])
- Each 2D chessboard corner yields two constraints on the 6-11 unknowns
- But, must also find 6 extrinsic parameters per image (rotation/translation)
- Result: Two or more images of a chessboard are sufficient

Learning OpenCV

Gary Bradski and Adrian Kaehler

O'REILLY®

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CHAPTER 11

Camera Models and Calibration

Vision begins with the detection of light from the world. That light begins as rays emanating from some source (e.g., a light bull or the sun), which then travels through space until striking some object. When that light strikes the object, much of the light is absorbed, and what is not absorbed we perceive as the color of the light. Reflected light at makes its way to our eye for our camera) is collected on our retial for our imager.) The geometry of this arrangement—particularly of the ray's travel from the object, through the lens in our eye or camera, and to the retina or imager—is of particular importance to practical computer vision.

portance to practical computer vision.

A simple but useful model of how this happens is the pinhole camera model.* A pinhole is an imaginary wall with a timy hole in the center that blocks all rays except those passing through the timy aperture in the center. In this chapter, we will start with a pinhole camera model to get a handle on the basis geometry of projecting rays. Unfortunately, a real pinhole is not a very good way to make images because it does not gather enough light for rapid exposure. This is why our eyes and cameras use lenses to gather more light than what would be available at a single point. The downside, however, is that gathering more light with a lens not only forces us to move beyond the simple geometry of the pinhole model but also introduces distortions from the lens itself.

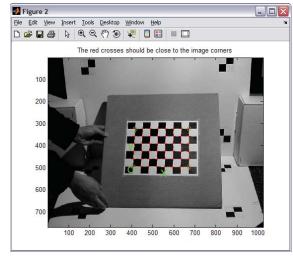
the pinnoise model total asio introduces distortions from the lens steet.

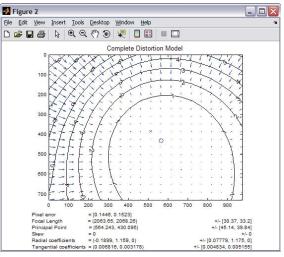
In this chapter we'll learn how, suiging camera calibration, to correct (mathematically) for the main deviations from the simple pinhole model that the use of lenses imposes on us. Camera calibration is important also for relating camera measurements with measurements in the real, three-dimensional world. This is important because scenes are not only three-dimensional, they are also physical spaces with physical until them, the relation between the camera's natural units (pixels) and the units of the

Scorology of these, you had a fact in Bount time. The globals center model per back at least 19 are and 4 (Them Bull 19 aid had believe we fittending by global powering agrees or discolous Authorities and and physical advances followed in the 160% and 170% with Deceaters, Argine, Gallien, Newton, Houke, Elent, Ferman, and Sould feet O'Conneil (Chronocoll), Some by produce tests for geometric vicion include those by Three, I Traccolly, Junique (and Anneilla, Marcell (Jackelle, Marcell), Hadwert (Marcell), Hadwert (Marcell

370

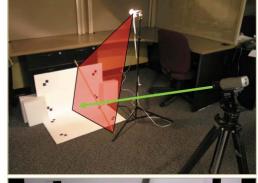
Demo: Camera Calibration in Matlab



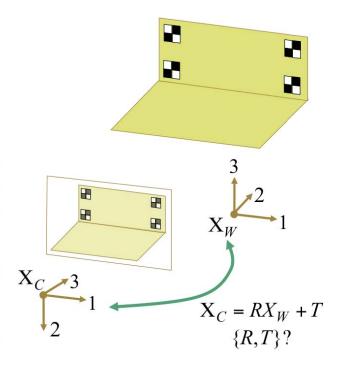


Camera Calibration Toolbox - Standard Version Read images Extract grid corners Calibration Image names Reproject on images Show Extrinsic Analyse error Recomp. corners Add/Suppress images Exit Comp. Extrinsic Undistort image Export calib data Show calib results

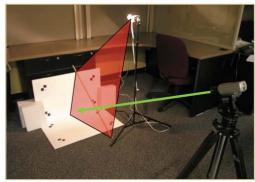
Extrinsic Camera Calibration



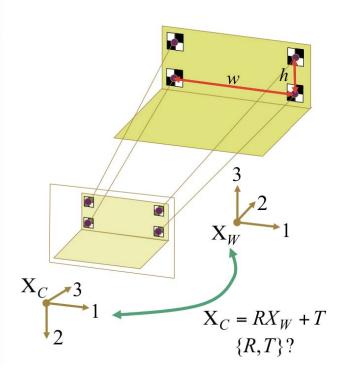




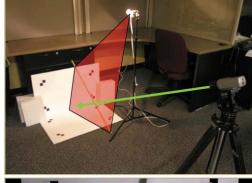
Extrinsic Camera Calibration



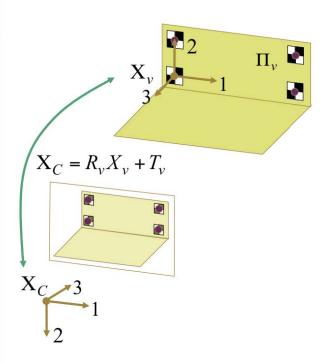




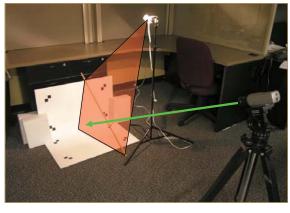
Extrinsic Camera Calibration

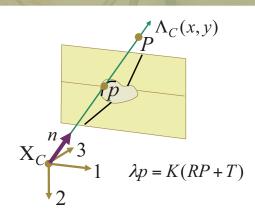






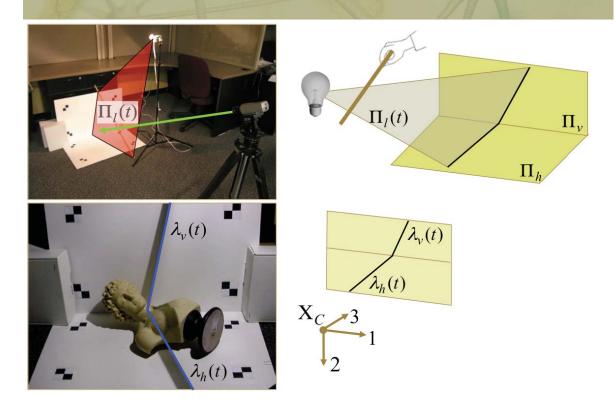
Demo: Mapping Pixels to Optical Rays



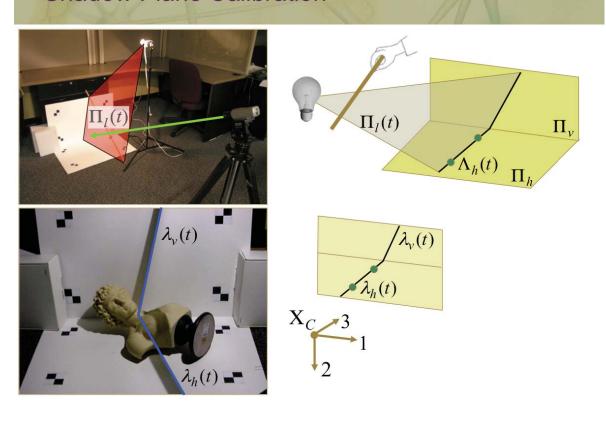


- How to map an image pixel to an optical ray?
- Solution: Invert the calibrated camera projection model
- But, also requires inversion of distortion model (which is non-linear)
- Mapping implemented in Camera Calibration Toolbox with normalize.m
- → Result: After calibration, pixels can be converted to optical rays

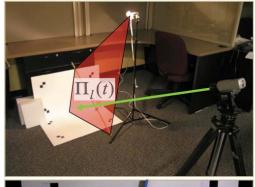
Shadow Plane Calibration

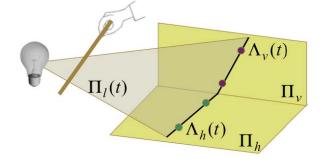


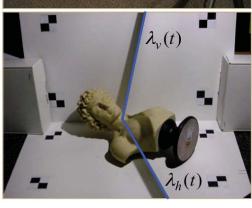
Shadow Plane Calibration

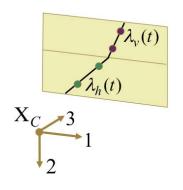


Shadow Plane Calibration

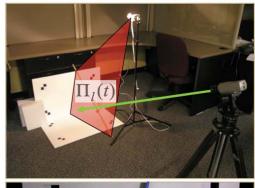


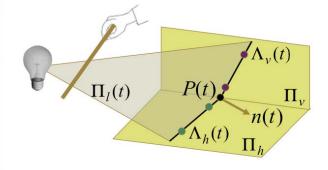


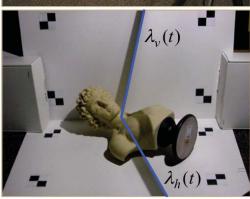


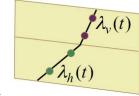


Shadow Plane Calibration







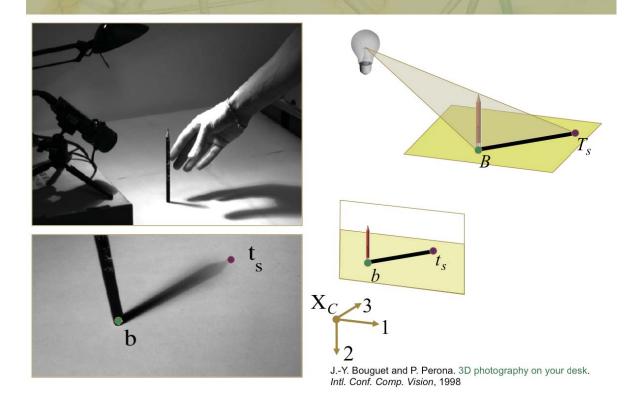


$$X_{C}$$
 3

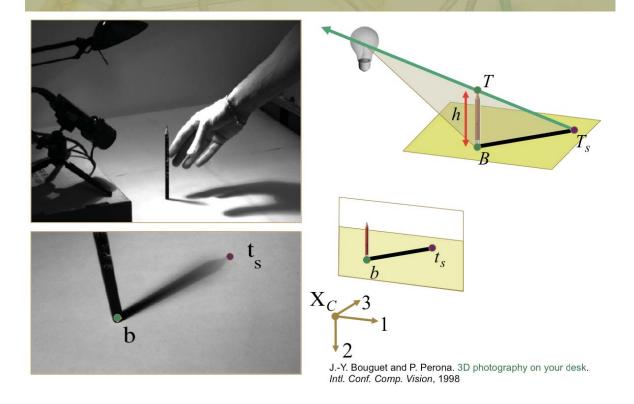
$$P(t) = \Lambda_h(t) \cap \Lambda_v(t)$$

$$n(t) = \Lambda_h(t) \otimes \Lambda_v(t)$$

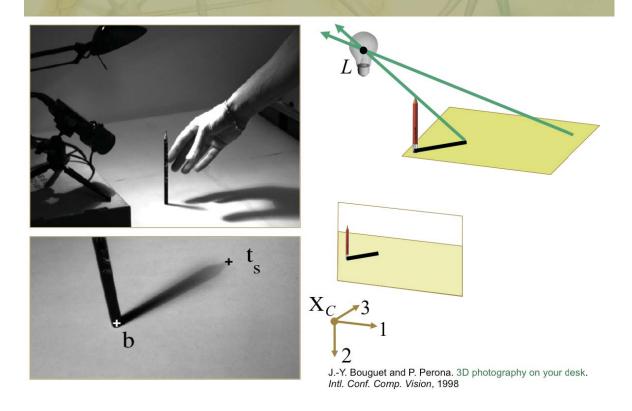
Alternatives for Shadow Plane Calibration



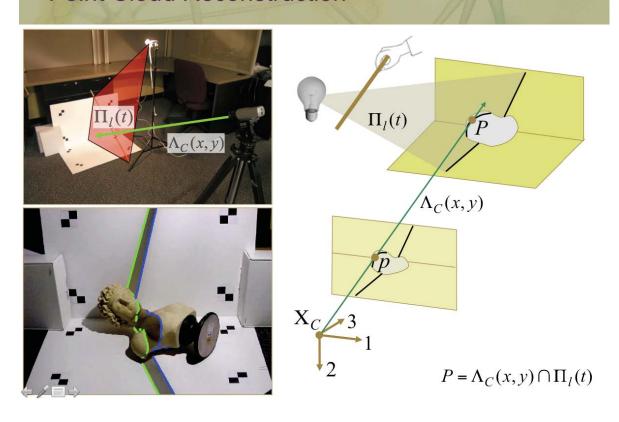
Alternatives for Shadow Plane Calibration



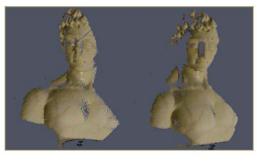
Alternatives for Shadow Plane Calibration

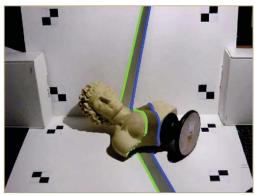


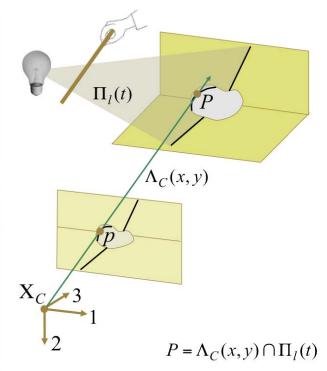
Point Cloud Reconstruction



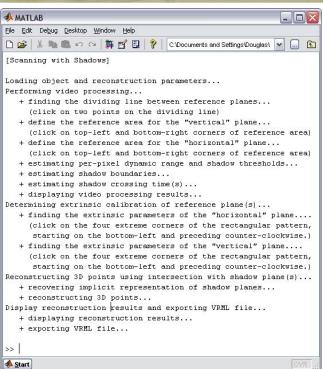
Point Cloud Reconstruction

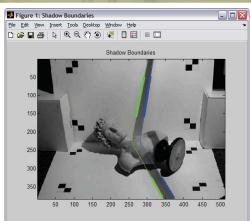






Demo: Putting it All Together





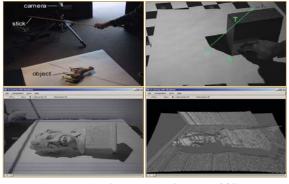


VRML File Format

Additional Reconstruction Examples



J.-Y. Bouguet and P. Perona. 3D photography on your desk. *Intl. Conf. Comp. Vision*, 1998



J. Kim and J. Wu. Scanning with Shadows. CSE 558 Project Report (U. Washington), 2001



P. Blaer, N. Hasan, C. Tripp, and L. Volchok. 3D Desktop Photography by Eclipse. Project Report (Columbia), 2001



J. Kubicky. Home-Brew 3-D Photography. EE 149 Project Report (Caltech), 1998

Course Schedule

- Introduction
- The Mathematics of 3D Triangulation
- 3D Scanning with Swept-Planes
- Camera and Swept-Plane Light Source Calibration
- > Reconstruction and Visualization using Point Clouds

Introducción a la Fotografia 3D UBA/FCEN Marzo 27 – Abril 12 2013 Clase 5 : Lunes Abril 8

Gabriel Taubin
Brown University

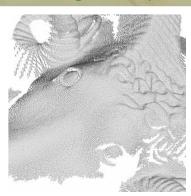


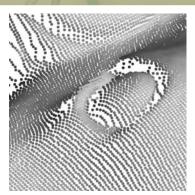
Course Schedule

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- Combining Point Clouds Recovered from Multiple Views

Visualizing Point Clouds: Point-based Rendering via Splatting

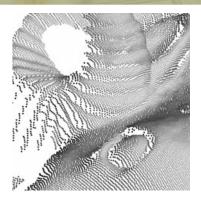






- Swept-plane scanner produces a colored point cloud: a set of 3D points
- Problem: how to render a point cloud to make it look like as a continuous surface?
- Splatting: render points as overlapping colored disks
- If normal vectors are measured as well, render points as shaded ellipses

Visualizing Point Clouds: Point-based Rendering via Splatting





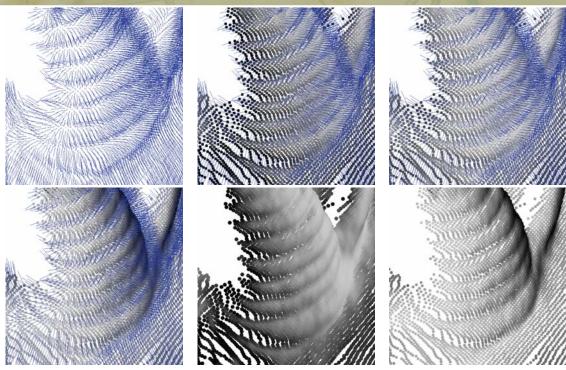


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^{*}See the SIGGRAPH 2009 course: Point Based Graphics – State of the Art and Recent Advances by Markus Gross.

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Visualizing Point Clouds: Splatting with normal vectors and colors



Visualizing Point Clouds: File Formats

- No standard file format to store point clouds
- Point = (x,y,z) plus (R,G,B) and/or (Nx,Ny,Nz)
- It is easy to create an ad-hoc file format
- Scene graph based file format: VRML
- International standard: ISO/IEC 14772-1:97 VRML' 97
- PointSet node includes coordinates (x,y,z) and optional colors (R,G,B), but no normals

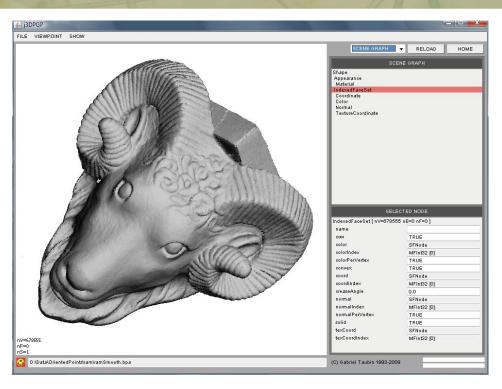
```
PointSet {
  coord Coordinate {
    point [
        0 -1 2, 1 0 0,
        -2 3 -1
      ]
  }
  color Color {
    color [
        1 0 0, 0 1 0, 1 1 0
      ]
  }
}
```

Visualizing Point Clouds: File Formats

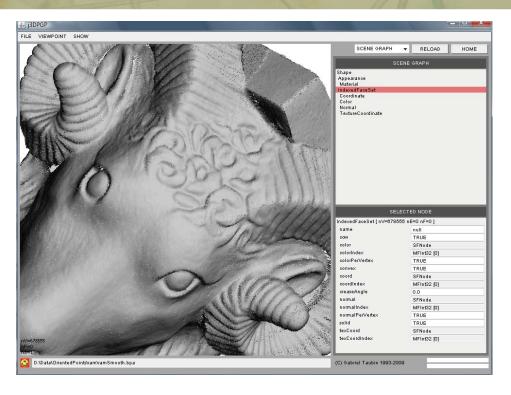
- IndexedFaceSet node designed to store a polygon mesh can be used to store point clouds with optional colors and/or normal vectors
- Store point coordinates as vertices
- Store point colors as colors per vertex
- Store point normal vectors as normals per vertex
- Degenerate polygon mesh with no faces is valid VRML syntax

```
IndexedFaceSet {
coord Coordinate {
point [
 0 -1 2,
 1 0 0,
 -2 3 -1
colorPerVertex TRUE
color Color {
color [
 100,
 0 1 0.
 110
normalPerVertex TRUE
normal Normal {
vector [
 100,
 0 1 0,
 001
```

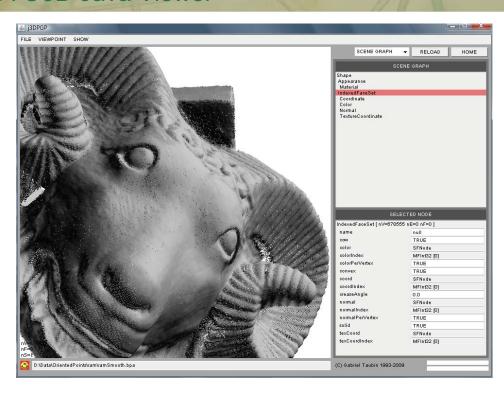
Visualizing Point Clouds: BYO3D Java Viewer



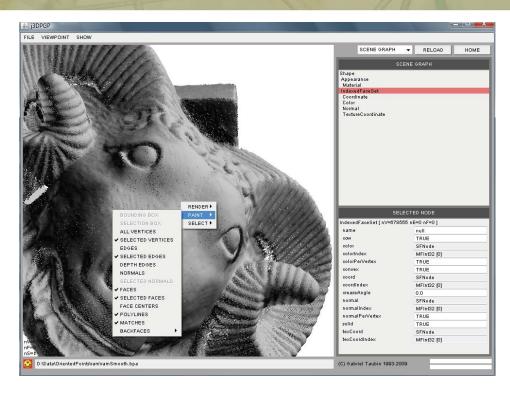
Visualizing Point Clouds: BYO3D Java Viewer



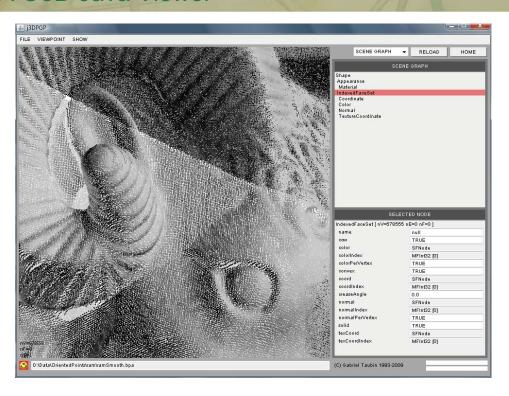
Visualizing Point Clouds: BYO3D Java Viewer



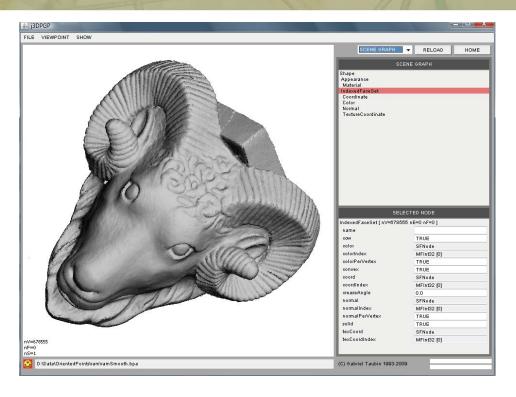
Visualizing Point Clouds: BYO3D Java Viewer



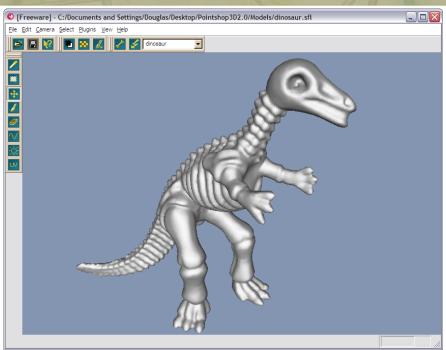
Visualizing Point Clouds: BYO3D Java Viewer



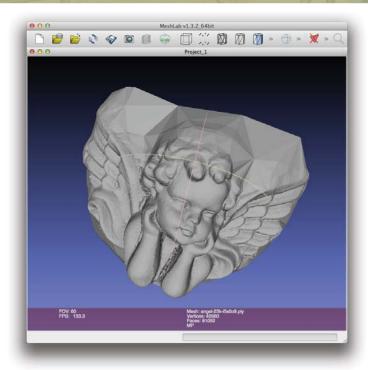
Visualizing Point Clouds: BYO3D Java Viewer

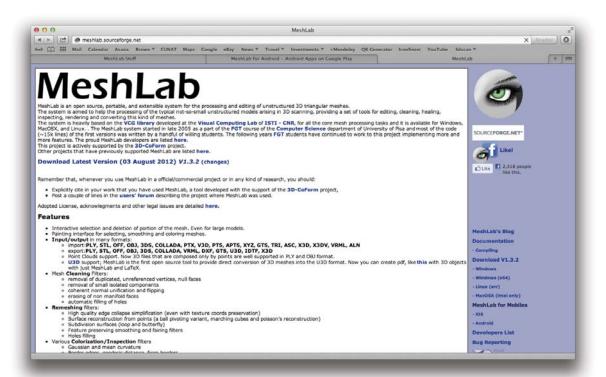


Visualizing Point Clouds: Pointshop 3D [Zwicker et al. 2002]



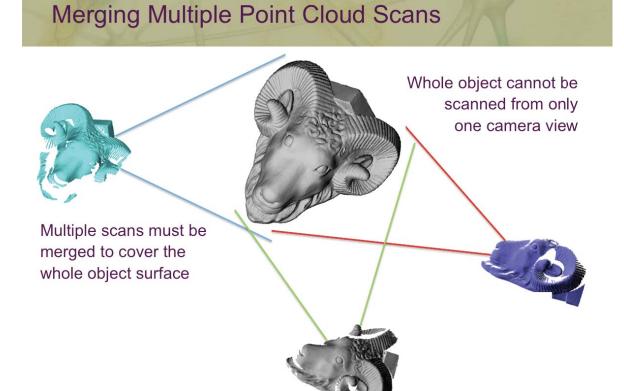
Visualizing Point Clouds: MeshLab



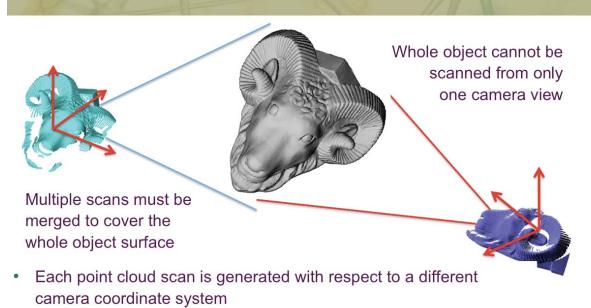


Course Schedule

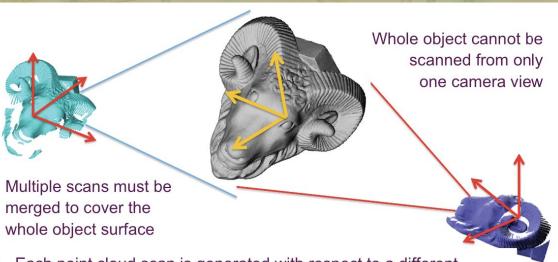
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Merging Multiple Point Cloud Scans

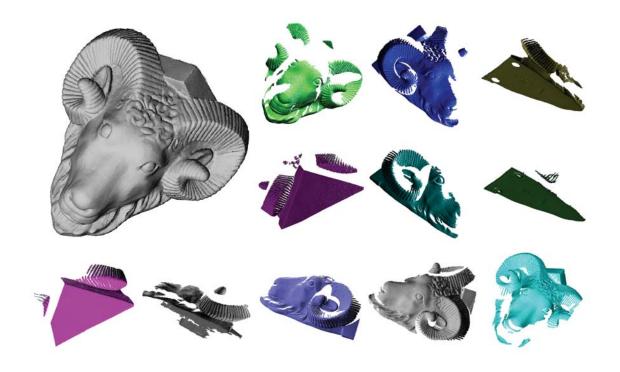


Merging Multiple Point Cloud Scans



- Each point cloud scan is generated with respect to a different camera coordinate system
- Relative position and orientation of each scan with respect to a global coordinate system must be determined to produce a single merged point cloud

Merging Point Cloud Scans



Complex Models May Require 100s of Scans

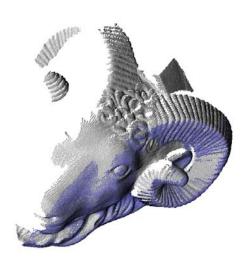




Merging Point Cloud Scans

- Incremental registration and merging
- Followed by global relaxation to remove accumulated errors

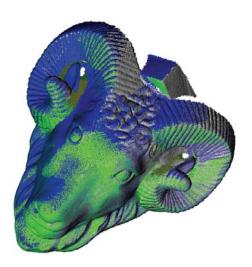




Merging Point Cloud Scans

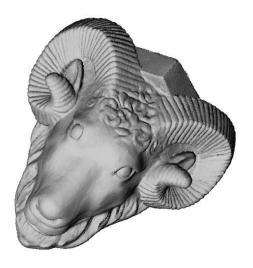
- Incremental registration and merging
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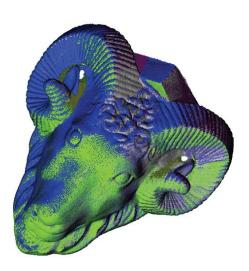




Merging Point Cloud Scans

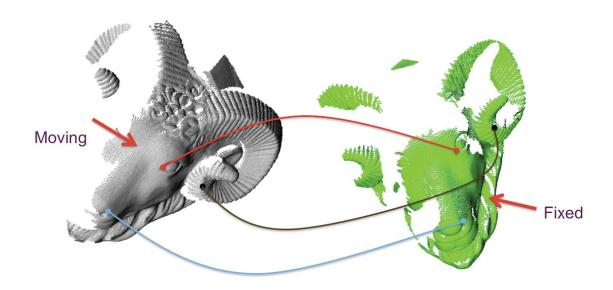
- Incremental registration and merging
- Followed by global relaxation to remove accumulated errors





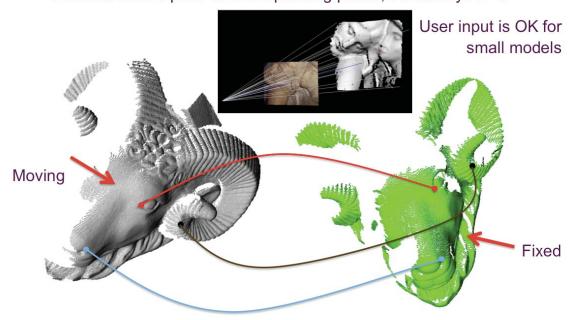
Merging Two Point Cloud Scans

Select at least 3 pairs of corresponding points, but ideally N>>3



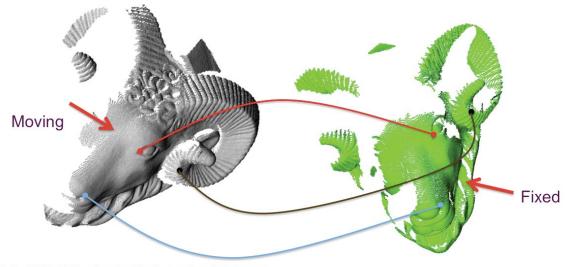
Merging Two Point Cloud Scans

Select at least 3 pairs of corresponding points, but ideally N>>3



Merging Two Point Cloud Scans

- Select at least 3 pairs of corresponding points, but ideally N>>3
- Solve in close form for the matching rigid body transformation
- Refine solution using the Iterative Closest Point Algorithm (ICP)



P. Besl, N.D. McKey, A method for Registration of 3D Shapes. IEEE Transactions on PAMI, 1992

Computing the Matching Transformation

• Given N pairs of corresponding 3D points $(p_1,q_1),...,(p_n,q_n)$ we are looking for a rotation matrix R and a translation vector T so that

$$Rp_j + T = q_j$$
 $j = 1,...,n$

- In general, solution does not exists: solve in the Least-Squares sense
- Now we are looking for the minimizer of the quadratic energy function

$$E(R,T) = \frac{1}{n} \sum_{j=1}^{n} ||Rp_{j} + T - q_{j}||^{2}$$

This problem has a closed form solution

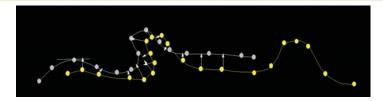
$$R = V^{t}U$$
, $T = \overline{q} - R\overline{p}$

Where

$$\overline{p} = \frac{1}{n} \sum_{j=1}^{n} p_{j} \quad \overline{q} = \frac{1}{n} \sum_{j=1}^{n} q_{j} \quad M = \frac{1}{n} \sum_{j=1}^{n} (p_{j} - \overline{p})(q_{j} - \overline{q})^{t}$$

• And $M = U\Delta V^t$ is the Singular Value Decomposition (SVD) of M

Iterative Closest Point Algorithm (ICP)



- 1. Automatically select N points $p_1,...,p_n$
- 2. Find closest corresponding points $q_1,...,q_n$
- 3. Solve in close form for the matching rigid body transformation which minimizes the energy function

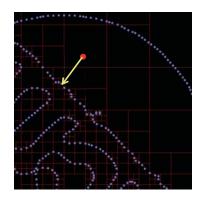
$$E(R,T) = \frac{1}{n} \sum_{j=1}^{n} ||Rp_{j} + T - q_{j}||^{2}$$

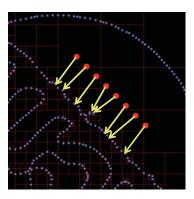
4. Repeat 1-3 while until convergence



Finding Closest Points

- Problem: find the point of the set $D = \{p_1, ..., p_n\}$ closest to the point q
- Naïve algorithm: sequential search O(N)
- Too expensive if the same computation must be performed for many points $q_1, ..., q_n$
- Efficient algorithm requires space partition data structure Quadtree/Octree, BSP tree





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Gabriel Taubin
Brown University

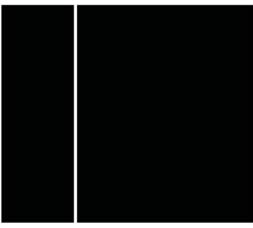


Course Schedule

- > Structured Lighting
- Projector Calibration and Structured Light Reconstruction

Structured Lighting: Swept-Planes Revisited

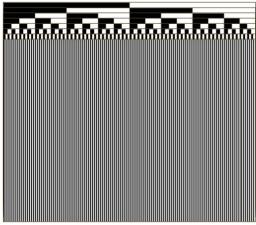




- Swept-plane scanning recovers 3D depth using ray-plane intersection
- Use a data projector to replace manually-swept laser/shadow planes
- How to assign correspondence from projector planes to camera pixels?
- Solution: Project a spatially- and temporally-encoded image sequence
- What is the optimal image sequence to project?

Structured Lighting: Binary Codes



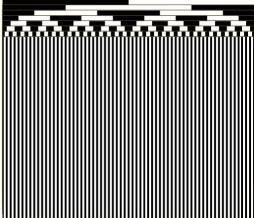


Binary Image Sequence [Posdamer and Altschuler 1982]

- Each image is a bit-plane of the binary code for projector row/column
- Minimum of 10 images to encode 1024 columns or 768 rows
- In practice, 20 images are used to encode 1024 columns or 768 rows
- Projector and camera(s) must be synchronized

Structured Lighting: Gray Codes





Gray Code Image Sequence [Inokuchi 1984]

- Each image is a bit-plane of the Gray code for each projector row/column
- Requires same number of images as a binary image sequence, but has better performance in practice

Bin2Gray(B,G)

- $1 G \leftarrow B$
- 2 for $i \leftarrow n-1$ downto 0
- $G[i] \leftarrow B[i+1] \text{ xor } B[i]$

Gray Codes: Decoding Performance



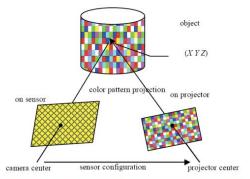




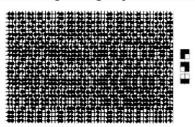
3D Reconstruction using Structured Light [Inokuchi 1984]

- Implemented using a total of 42 images
 (2 to measure dynamic range, 20 to encode rows, 20 to encode columns)
- Individual bits assigned by detecting if bit-plane (or its inverse) is brighter
- Decoding algorithm: Gray code → binary code → integer row/column index

Additional Structured Lighting Patterns



Spatial encoding strategies [Chen et al. 2007]



Pseudorandom and M-arrays [Griffin 1992]

J. Salvi, J. Pagès, and J. Batlle. Pattern Codification Strategies in Structured Light Systems. *Pattern Recognition*, 2004







"Single-shot" patterns (N-arrays, grids, random, etc.)

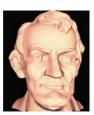




De Bruijn sequences [Zhang et al. 2002]







Phase-shifting [Zhang et al. 2004]

Assembling Your Own Scanner



Parts List [\$600-\$800, but only \$300 without mounting hardware]

- [1] Camera (Logitech QuickCam Pro 9000) [\$70]
- [1] Projector (InFocus LP 70+) [\$200-\$400 from eBay]
- [1] Manfrotto 190XB 3 Section Aluminum Tripod [\$130]
- [1] Manfrotto 486RC2 Compact Ball Head [\$75]
- [1] Custom Aluminum Rail (with 3/8 inch holes for mounting ball heads) [NA]
- [1] Custom Aluminum Tripod Adaptor Plate (for mounting projector to ball head) [NA]
- [2] Manfrotto 484 Mini Ball Heads [\$45 each]
- [1] Sunpak 620-500C Versipod (with adjustable, locking ball head) [\$15]
- [1] ~11x17 inch foamcore board (with an affixed calibration chessboard) [\$10]

Assembling Your Own Scanner







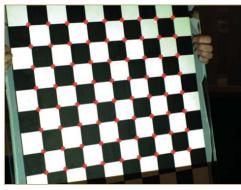
Parts List [\$600-\$800, but only \$300 without mounting hardware]

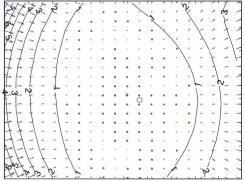
- [1] Camera (Logitech QuickCam Pro 9000) [\$70]
- [1] Projector (InFocus LP 70+) [\$200-\$400 from eBay]
- [1] Manfrotto 190XB 3 Section Aluminum Tripod [\$130]
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- [1] ~11x17 inch foamcore board (with an affixed calibration chessboard) [\$10]

Developing Your Own Software

Key Functions

Camera and projector calibration





Developing Your Own Software

Key Functions

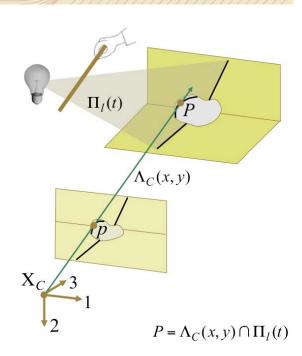
- Camera and projector calibration
- Camera and projector interfaces



Developing Your Own Software

Key Functions

- Camera and projector calibration
- Camera and projector interfaces
- Geometric operations



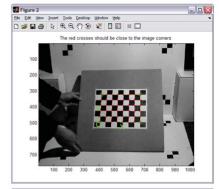
Developing Your Own Software

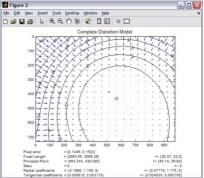
Key Functions

- Camera and projector calibration
- Camera and projector interfaces
- Geometric operations

Matlab

 Camera Calibration Toolbox (updated to support projector calibration)





Developing Your Own Software

Key Functions

- Camera and projector calibration
- Camera and projector interfaces
- Geometric operations

Matlab

- Camera Calibration Toolbox (updated to support projector calibration)
- Projector-Camera Calibration Toolbox (just released, supports full calibration)





Developing Your Own Software

Key Functions

- Camera and projector calibration
- Camera and projector interfaces
- Geometric operations

Matlab

- Camera Calibration Toolbox (updated to support projector calibration)
- Projector-Camera Calibration Toolbox (just released, supports full calibration)
- Image Acquisition Toolbox, etc.
- Geometric operations (course source)





http://code.google.com/p/procamcalib/

Developing Your Own Software

Key Functions

- Camera and projector calibration
- Camera and projector interfaces
- Geometric operations

Matlab

- Camera Calibration Toolbox (updated to support projector calibration)
- Projector-Camera Calibration Toolbox (just released, supports full calibration)
- Image Acquisition Toolbox, etc.
- Geometric operations (course source)

OpenCV

- Supports camera calibration
- Updated to support projector calibration (course source)



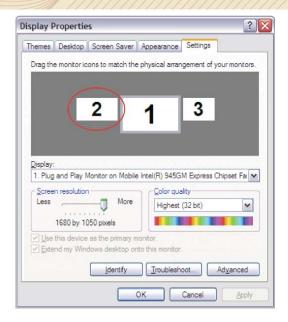


http://opencv.willowgarage.com/wiki/

Controlling a Projector for Structured Lighting

Operating System

A projector is just another display...



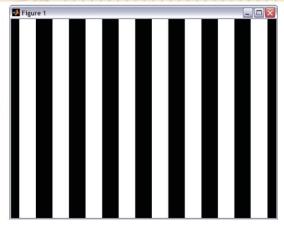
Controlling a Projector for Structured Lighting

Operating System

A projector is just another display...

Matlab

 Fullscreen display not fully supported (cannot remove window decorations)



```
imagesc(P{1}(:,:,5));
axis image off;
set(gca,'Pos',[0 0 1 1]);
set(gcf,'MenuBar','none');
set(gcf,'Pos',[-1023 283 1024 768]);
```

Controlling a Projector for Structured Lighting

Operating System

A projector is just another display...

Matlab

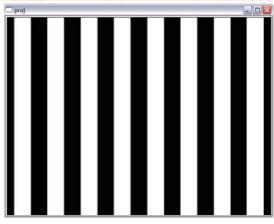
- Fullscreen display not fully supported (cannot remove window decorations)
- Use Java to control displays (slow, multiple display problems)
- Use the Psychophysics Toolbox (Screen.m wraps OpenGL functions)

OpenCV

- Cannot remove window decorations
- cvNamedWindow/cvMoveWindow

General

Use OpenGL wrappers



```
cvNamedWindow("proj",CV_WINDOW_AUTOSIZE);
IplImage* proj_frame =
    cvCreateImage(cvSize(w,h),8,3);
cvSet(proj_frame,cvScalar(0,0,0));
cvShowImage("proj",proj_frame);
cvMoveWindow("proj",-w-7,-33);
cvWaitKey(1);
```

http://opencv.willowgarage.com/wiki

Course Schedule

- Structured Lighting
- > Robust Pixel Classification
- Projector Calibration / Structured Light Reconstruction
- Surface Reconstruction from Point Clouds
- Elementary Mesh Processing

Robust Pixel Classification





- Robust pixel classification for 3d modeling with structured light, by Yi Xu and Daniel G. Aliaga, in Proceedings of Graphics Interface 2007, GI '07, pages 233–240, New York, NY, USA, 2007. ACM.
- Fast separation of direct and global components of a scene using high frequency illumination, by Shree K. Nayar, Gurunandan Krishnan, Michael D. Grossberg, and Ramesh Raskar, in ACM Trans. Graph., 25(3):935–944, July 2006.

Robust Pixel Classification

- The intensity of a pixel can be decomposed into the direct component and indirect (or global) component.
- The direct component is due to light bouncing off the surface in a single reflection.
- The indirect component is due to multiple reflections (e.g. inter-reflections, subsurface, scattering etc.).

$$L(p) = \begin{cases} L_d(p) + \alpha L_g(p) & \text{if p is on} \\ (1 - \alpha) L_g(p) & \text{if p is off,} \end{cases}$$

• where $0 \le \alpha \le 1$ is a fraction of activated source pixels. For example, for a random binary pattern $\alpha = 1$, and for a white pattern $\alpha = 1$.

Robust Pixel Classification

- Estimate direct and global components for each pixel using the method by Nayar
- Use two images of the scene, one with the scene lit with high-frequency illumination, and the other lit with the complementary illumination.

$$L_d(p) = L_{max}(p) - \frac{\alpha}{1 - \alpha} L_{min}(p)$$
$$L_g(p) = \frac{1}{1 - \alpha} L_{min}(p),$$

Robust Pixel Classification

- Projecting the code pattern i and its inverse yields two values for each pixel.
- Classify p according to the rules

$$p \text{ is } \begin{cases} \text{uncertain} & \text{if } L_d(p) < m \\ \text{on} & \text{if } L_d(p) > L_g(p) \text{ and } L_i^+(p) > L_i^-(p) \\ \text{off} & \text{if } L_d(p) > L_g(p) \text{ and } L_i^+(p) < L_i^-(p) \\ \text{off} & \text{if } L_i^+(p) < L_d(p) \text{ and } L_i^-(p) > L_g(p) \\ \text{on} & \text{if } L_i^+(p) > L_g(p) \text{ and } L_i^-(p) < L_d(p) \\ \text{uncertain} & \text{otherwise,} \end{cases}$$

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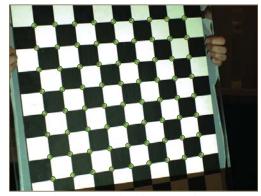
Gabriel Taubin
Brown University



Course Schedule

- Structured Lighting
- Robust Pixel Classification
- > Projector Calibration / Structured Light Reconstruction
- Projector Calibration / Structured Light Reconstruction
- Surface Reconstruction from Point Clouds
- Elementary Mesh Processing

Summary of Camera Calibration



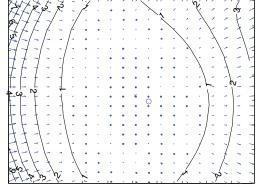


Image Sequence for Camera Calibration

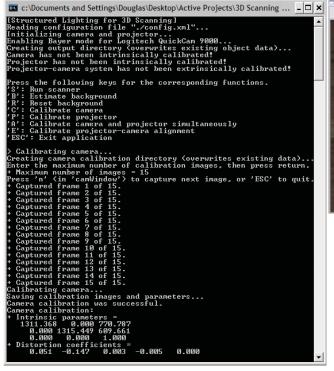
Estimated Camera Lens Distortion

Camera Calibration Procedure

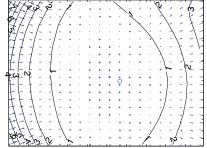
Use the Camera Calibration Toolbox for Matlab or OpenCV

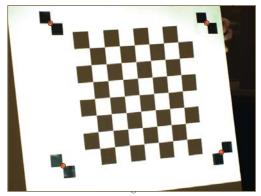
Normalized Ray	Distorted Ray (4 th -order radial + tangential)	Predicted Image-plane Projection
$\mathbf{x}_{n} = \begin{bmatrix} \mathbf{X}_{c} / \mathbf{Z}_{c} \\ \mathbf{Y}_{c} / \mathbf{Z}_{c} \end{bmatrix} = \begin{bmatrix} \mathbf{x} \\ \mathbf{y} \end{bmatrix}$	$x_{d} = \begin{bmatrix} x_{d}(1) \\ x_{d}(2) \end{bmatrix} = (1 + kc(1) r^{2} + kc(2) r^{4} + kc(5) r^{6}) x_{n} + dx$ $dx = \begin{bmatrix} 2 kc(3) x y + kc(4) (r^{2} + 2x^{2}) \\ kc(3) (r^{2} + 2y^{2}) + 2 kc(4) x y \end{bmatrix}$	$x_{p} = fc(1) (x_{d}(1) + alpha_{e} * x_{d}(2)) + cc(1)$ $y_{p} = fc(2) x_{d}(2) + cc(2)$

Demo: Camera Calibration in OpenCV



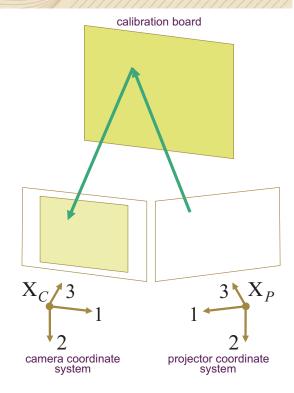




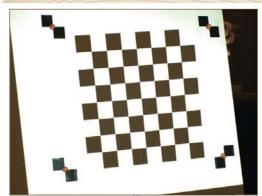


Calibration Procedure

 Consider projector an inverse camera (maps intensities to 3D rays)

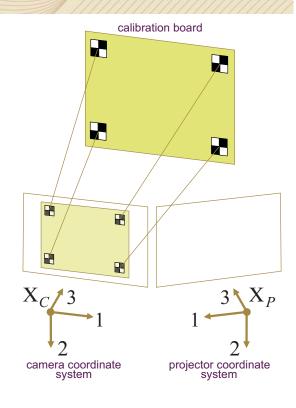


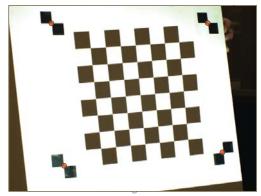
Projector Calibration



Calibration Procedure

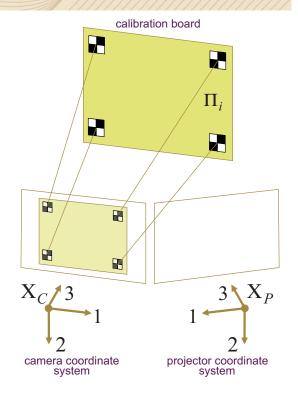
- Consider projector an inverse camera (maps intensities to 3D rays)
- Identify printed fiducials in each image



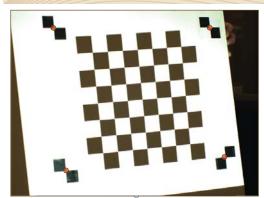


Calibration Procedure

- Consider projector an inverse camera (maps intensities to 3D rays)
- Identify printed fiducials in each image
- Use fidicials to find 3D calibration plane

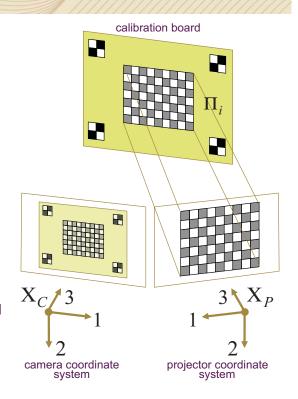


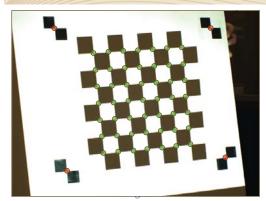
Projector Calibration



Calibration Procedure

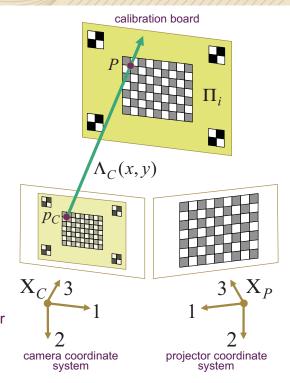
- Consider projector an inverse camera (maps intensities to 3D rays)
- Identify printed fiducials in each image
- Use fidicials to find 3D calibration plane
- Project checkerboard on calibration board



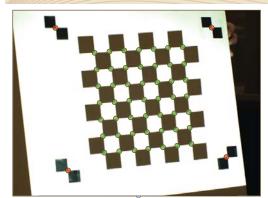


Calibration Procedure

- Consider projector an inverse camera (maps intensities to 3D rays)
- Identify printed fiducials in each image
- Use fidicials to find 3D calibration plane
- Project checkerboard on calibration board
- Find ray-plane intersection for each corner

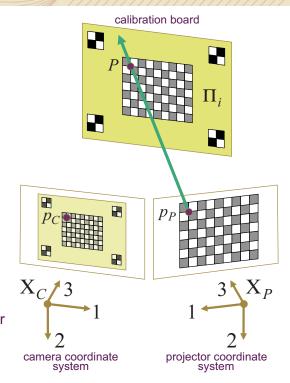


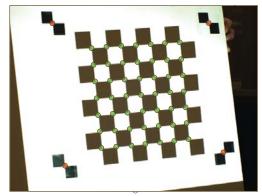
Projector Calibration



Calibration Procedure

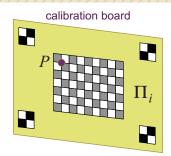
- Consider projector an inverse camera (maps intensities to 3D rays)
- Identify printed fiducials in each image
- Use fidicials to find 3D calibration plane
- Project checkerboard on calibration board
- Find ray-plane intersection for each corner

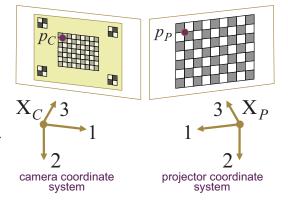




Calibration Procedure

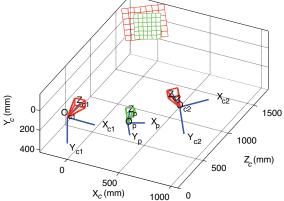
- Consider projector an inverse camera (maps intensities to 3D rays)
- Identify printed fiducials in each image
- Use fidicials to find 3D calibration plane
- Project checkerboard on calibration board
- Find ray-plane intersection for each corner
- Use 2D→3D correspondences to estimate intrinsic/extrinsic projector calibration (and radial distortion model)





Projector-Camera Calibration Results

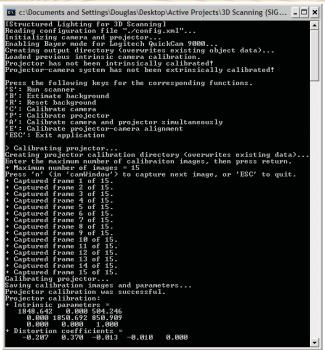


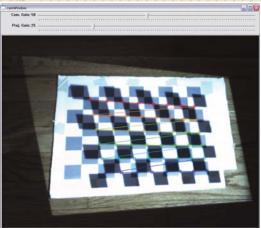


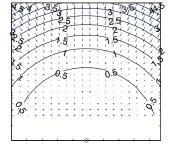
Projector-Camera Calibration Results

- Implemented complete toolbox for projector-camera calibration (available for Matlab and OpenCV)
- Sufficient accuracy for structured lighting applications
- Software and documentation available on the course website

Demo: Projector Calibration in OpenCV

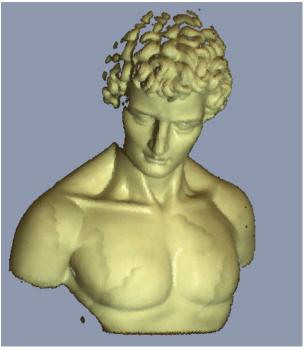






Structured Lighting Reconstruction Results





Additional Reconstruction Examples



Demo: Putting it All Together

```
Istructured Lighting for 3D Scanning | Xeanning | Xeading configuration file "./config.xml"...
Initializing camera and projector...
Enabling Bayer mode for Logitech QuickCan 9000...
Creating output directory (overwrites existing object data)...
Loaded previous intrinsic camera calibration.
Loaded previous intrinsic projector calibration.
Loaded previous extrinsic projector calibration.
Loaded previous extrinsic projector calibration.

Press the following keys for the corresponding functions.

'S': Run scanner
'B': Estimate background
'C': Calibrate camera
'P': Calibrate camera
'P': Calibrate camera and projector simultaneously
'E': Calibrate camera and projector simultaneously
'E': Calibrate then press any key (in 'camWindow') to scan.
Displaying the structured light sequence...
Remove object. then press any key (in 'camWindow') to scan.
Displaying the structured light sequence...
Reconstructing the point cloud and the depth map...

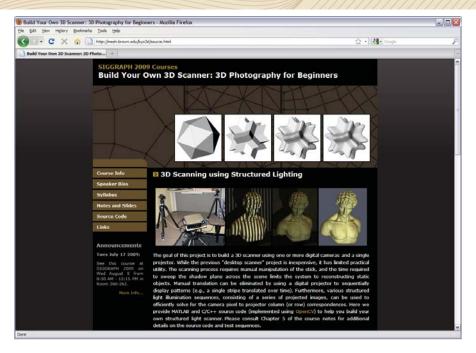
Press the following keys for the corresponding functions.

'S': Run scanner
'P': Estimate background
'R': Reset background
'C': Calibrate camera and projector simultaneously
'E': Calibrate camera and projector simultaneously
'E': Calibrate projector
'P': Estimate projector simultaneously
'E': Calibrate camera and projector simultaneously
'E': Calibrate projector
'P': Estimate projector simultaneously
'E': Calibrate camera and projector simultaneously
'E': Calibrate projector
'B': Calib
```



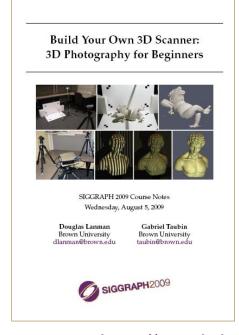


How to Get the Source Code



http://mesh.brown.edu/byo3d

For More Details



Chapter 5

Structured Lighting

In this chapter we describe how to build a structured light scanner using one or more digital cameras and a single projector. While the "desktop scanner" IEPI implemented in the previous chapter is inexpensive, it has limited practical utility. The scanning process requires manual manipulation of the stick, and the time required to sweep the shadow plane across the scene limits the system to reconstructing static objects. Manual translation can be eliminated by using a digital projector to sequentially display patterns (e.g., a single stipe translated over time). Furthermore, various structured light illumination sequences, consisting of a series of projected images, can be used to efficiently solve for the camera pixel to projector column (or row) correspondences.

images, can be used to efficiently solve for the camera pixel to projector column (or row) correspondences.

By implementing your own structured light scanner, you will directly extending the algorithms and software developed for the sweep-plane systems in the previous chapter. Reconstruction will again be accomplished using ray-plane triangulation. The key difference is that correspondences will now be established by decoding certain structured light sequences. At the time of writing, the software accompanying this chapter was developed in MATLAB. We encourage the reader to download that version, as well as any updates, from the course website at http://mesh.brown.edu/dlanman/scan3d.

5.1 Data Capture

5.1.1 Scanner Hardware

As shown in Figure 5.1, the scanning apparatus contains one or more digital cameras and a single digital projector. As with the swept-plane systems,

45

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Gabriel Taubin
Brown University

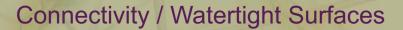


Course Schedule

- Structured Lighting
- Projector Camera Calibration
- > Surface Reconstruction from Point Clouds
- Elementary Mesh Processing
- Related Projects
- Conclusion / Q & A

Surface Representations

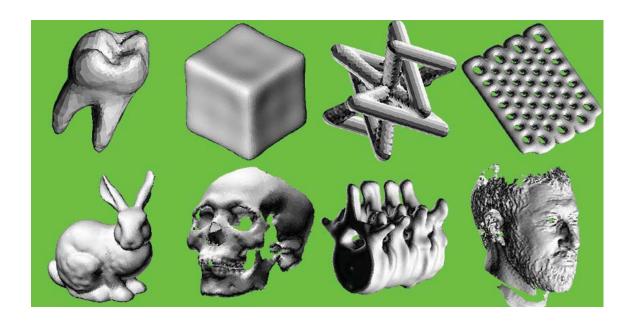
- Surfaces in Mathematics
 - Parametric $S = \{p = x(u) : u = (u_1, u_2) \in \mathbb{R}^2\}$
 - Implicit $S = \{p : f(p) = 0\}$ $f : V \to R$ $V \subset R^3$ (level set)
- We can only operate on a surface representation
 - A data structure defined by a finite number of parameters
 - · Efficient to perform certain geometric operations
- Point clouds (surfaces represented as sets of samples)
 - Positions
 - · Optional properties: normals, colors, etc
- Polygon meshes (piecewise planar surfaces)
 - vertices, edges, and faces
 - Optional properties: normals, color, texture coordinates, etc.



- Most applications require connectivity information
 - Efficient ways to find points in close proximity to each other
- Point clouds do not provide connectivity information
 - Additional data structures are needed to efficiently find neighboring points
- · Connectivity is explicit in polygon meshes: edges
- Triangulate the point cloud to get connectivity information
 - Find an interpolating or approximating triangle mesh
- Many applications require watertight surfaces: continuous closed surfaces which partition 3D space into an inside and an outside
 - Point clouds are not watertight
 - Polygon meshes may be watertight
- Will the triangulation constructed from the point cloud be watertight?

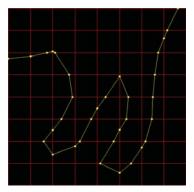


Polygon Meshes

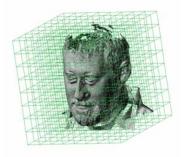


Surface Reconstruction from Point Clouds

- Every regular **Implicit surface** is watertight $S = \{p : f(p) = 0\}$
- An **Isosurface** is a polygonal approximation of an implicit function associated with a volumetric grid



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- An Isosurface is a polygonal approximation of an implicit function associated with a volumetric grid
- Marching Cubes is an algorithm to compute an isosurface from an implicit surface evaluated on the vertices of a regular hexahedral grid



W.E. Lorensen, H.E. Cline. Marching Cubes: A high resolution 3D surface reconstruction algorithm. Siggraph, 1987

Surface Reconstruction from Point Clouds

- Every regular **Implicit surface** is watertight $S = \{p : f(p) = 0\}$
- An Isosurface is a polygonal approximation of an implicit function associated with a volumetric grid
- Marching Cubes is an algorithm to compute an isosurface from an implicit surface evaluated on the vertices of a regular hexahedral grid
- Similar simple algorithms exists to generate isosurfaces from an implicit function evaluated on the vertices of a tetrahedral grid
- We will only discuss here approximation algorithms to fit implicit surfaces to point clouds
- Algorithms related to the Poisson Equation

W.E. Lorensen, H.E. Cline. Marching Cubes: A high resolution 3D surface reconstruction algorithm. Siggraph, 1987

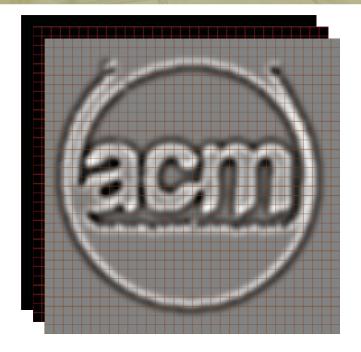


Oriented points

Curve Reconstruction from Point Clouds

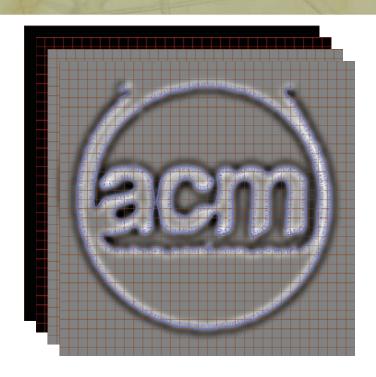


- Oriented points
- Regular grid

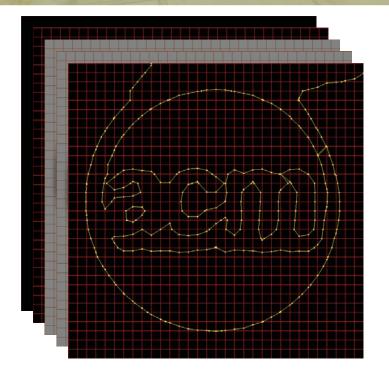


- Oriented points
- Regular grid
- Implicit function

Curve Reconstruction from Point Clouds

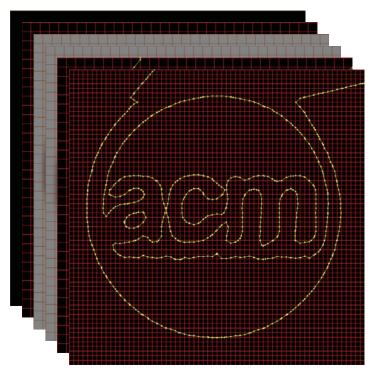


- Oriented points
- Regular grid
- Implicit function

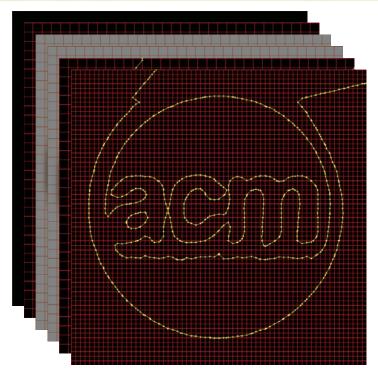


- Oriented points
- Regular grid
- Implicit function
- Isocurve

Curve Reconstruction from Point Clouds



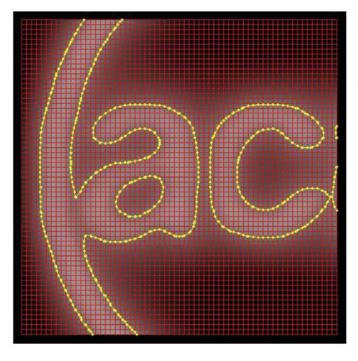
- Oriented points
- Regular grid
- Implicit function
- Isocurve
- Grid too coarse: Aliasing
- Finer grid resolves topology



- Oriented points
- Regular grid
- · Implicit function
- Isocurve
- Grid too coarse: Aliasing
- Finer grid resolves topology



IsoCurves



Given a continuous function

$$f(x_1,x_2)$$

· Sampled on a regular grid

$$G = (V, E, C)$$

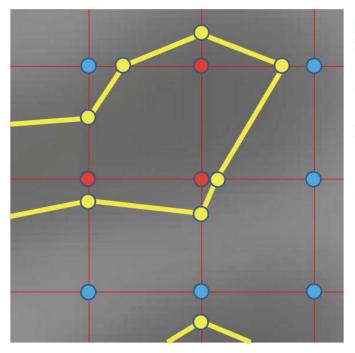
$$F = \{f_v : v \in V\}$$

 Compute a polygonal approximation of a level set

$$C_{\lambda} = \{x : f(x) = \lambda\}$$

 Increase grid resolution if necessary

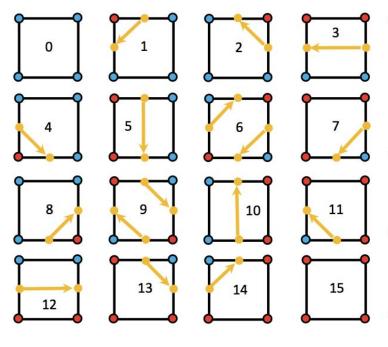
The Marching Lines Algorithm (ML)



4 STEPS

- Determine grid vertex sign bits
- Determine supporting grid edges
- Compute location of Isovertices along supporting grid edges
- Interconnect isovertices by table look-up within each cell

The Marching Lines Table



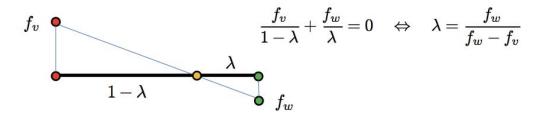
4 STEPS

- Determine grid vertex sign bits
- Determine supporting grid edges
- Compute location of Isovertices along supporting grid edges
- Interconnect isovertices by table look-up within each cell

Choices for 6 & 9

The 4 Steps

- 1. Determine grid vertex sign bits $b_v = egin{cases} 1 & f_v \geq 0 \ 0 & f_v < 0 \end{cases}$
- 2. Determine supporting grid edges $b_v \neq b_v$
- 3. Compute location of IsoVertices along supporting grid edges

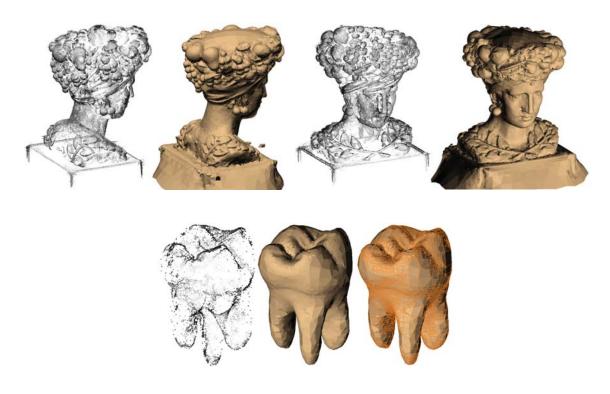


4. Interconnect IsoVertices by table look-up within each cell

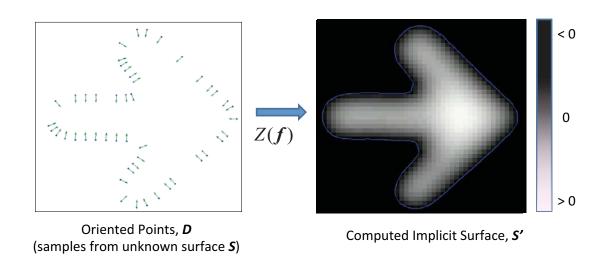
Related Papers & Projects

- Vector Field Isosurface-Based Reconstruction From Oriented Points, by Sibley & Taubin, Siggraph 2005 (Sketch).
- Smooth Signed Distance Surface Reconstruction, by Calakli & Taubin, PG 2011 & Computer Graphics Forum 2011.
- Smooth Signed Distance Colored Surface Reconstruction, by Calakli & Taubin, chapter in State-of-the-Art Volume on Computer Graphics, Visualization, Visual Analytics, VR and HCl, 2012.
- Accurate 3D Footwear Impression Recovery from Photographs, by Andalo, Calakli, Taubin, and Goldenstein, Proceedings of the 4th. International Conference on Imaging for Crime Detection and Prevention (ICDP-2011).
- High Resolution Surface Reconstruction from Multi-view Aerial Imagery, Calakli, Ulusoy, Restrepo, Mundy & Taubin, 3DIMPVT 2012
- REVEAL Digital Archaeology Project
- Cuneiform Automatic Translation Project

Particularly Good at Extrapolating Missing Data



Implicit function framework



Find a scalar valued function $f:D \to \Re$, whose zero level set $\mathbf{Z}(\mathbf{f}) = \mathbf{S'}$ is the estimate for true surface \mathbf{S}

Implicit Curve and Surface Reconstruction

• Input: oriented point set:

$$D = \{ (\mathbf{p_i}, \mathbf{n_i}) = 1,...,N \}$$

contained in a bounding volume V

• Output: implicit surface

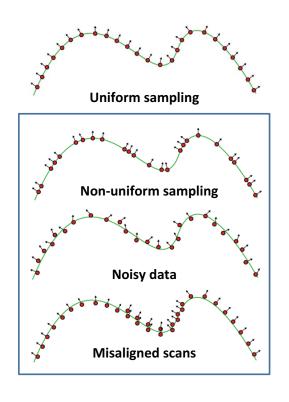
$$S = \{ \mathbf{x} \mid f(\mathbf{x}) = 0 \}$$

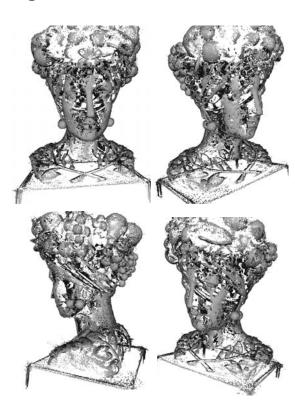
with the function defined on V, such that

$$f(\mathbf{p_i}) = 0$$
 and $\nabla f(\mathbf{p_i}) = \mathbf{n_i} \ \forall (\mathbf{p_i}, \mathbf{n_i}) \subseteq D$

- A family of implicit functions with a finite number of parameters has to be chosen
- Parameters must be estimated so that the conditions stated above are satisfied, if not exactly, then in the least-squares sense

Challenges





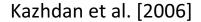
General Approaches

- Interpolating polygon meshes
 Boissonnat [1984], Edelsbrunner [1984]
 Amenta et al. [1998], Bernardini et al. [1999]
 Dey et al. [2003][2007], ...
- Implicit function fitting

 Taubin [1991], Hoppe et al. [1992], Curless et al. [1996]
 Whitaker [1998], Carr et al. [2001], Davis et al. [2002],
 Ohtake et al. [2004], Turk et al. [2004], Shen et al. [2004]
 Sibley-Taubin [2005]

Poisson Surface Reconstruction







Manson et al. [2008]

Poisson Surface Reconstruction

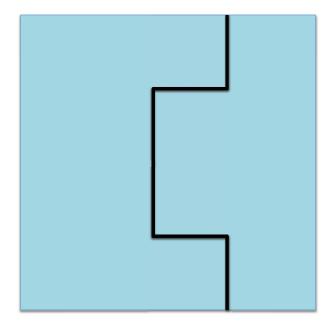
- 1. Extend oriented points to continuous vector field v(p) defined on the whole volume, so that $v(\mathbf{p_i}) \approx n_i$
- 2. Integrate vector field, by minimizing

$$\int_{V} \|\nabla f(p) - v(p)\|^2 dp$$

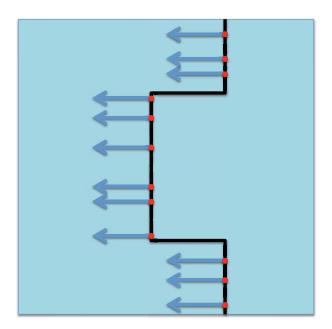
3. Determine isolevel, by minimizing

$$\sum_{i=1}^{N} (f(\mathbf{p_i}) - f_0)^2$$

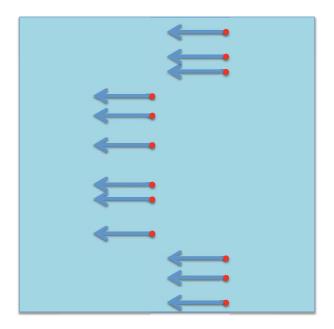
Main problem with this approach



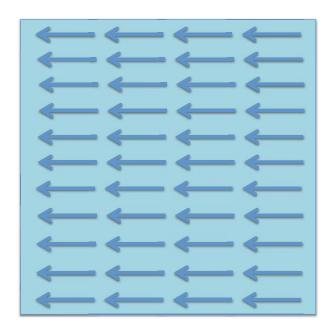
Main problem with this approach



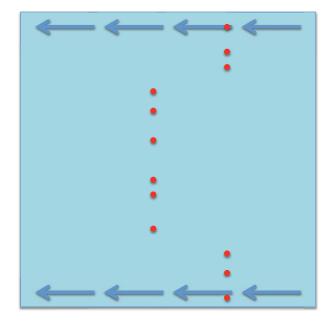
Main problem with this approach



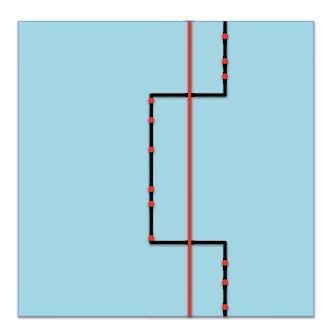
Main problem with this approach



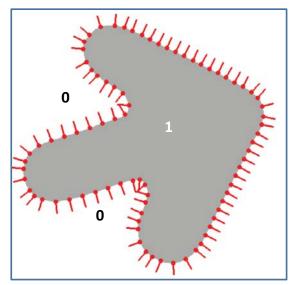
Main problem with this approach



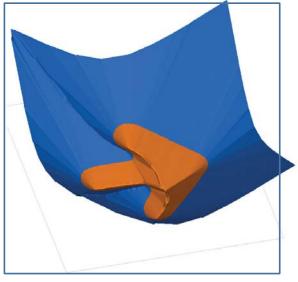
Main problem with this approach



What kind of implicit function?



Indicator Function

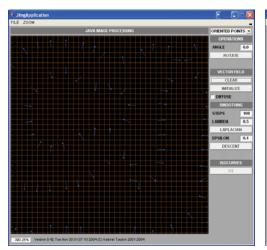


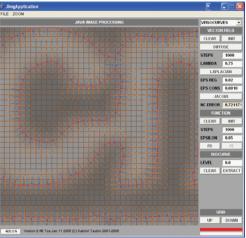
Smooth Signed Distance Function

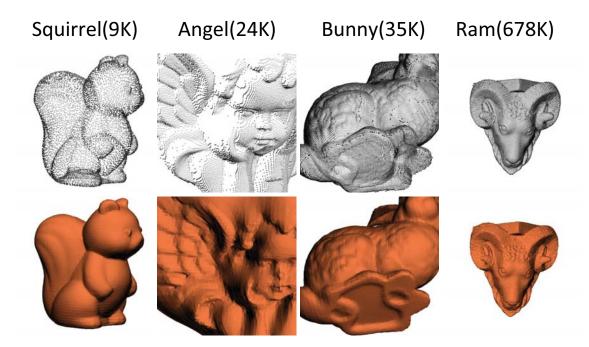
Vectorfield Isosurface-Based Reconstruction From Oriented Points

P. Sibley and G. Taubin [Siggraph 2005 Sketch]

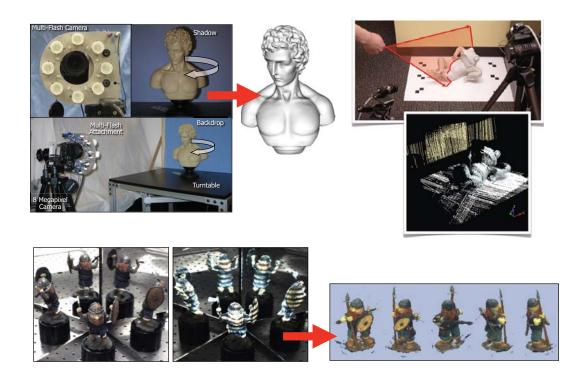
- Surface reconstruction from cloud of oriented points
- Implicit representation can deal with missing data
- Rather than fitting analytic function (RBFs, etc), and then extract isosurface for visualization, fit isosurface directly to data





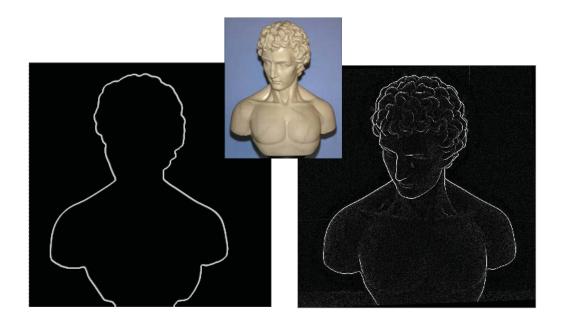


Some Methods to Capture 3D Point Clouds



Beyond Silhouettes: Surface Reconstruction using Multi-Flash Photography

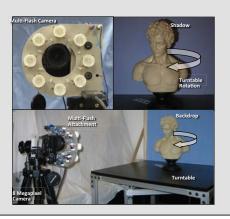
D. Crispell, D. Lanman, P. Sibley, Y. Zhao and G. Taubin [3DPVT 2006]



Multi-Flash 3D Photography: Capturing the Shape and Appearance of 3D Objects

A new approach for reconstructing 3D objects using shadows cast by depth discontinuities, as detected by a multi-flash camera. Unlike existing stereo vision algorithms, this method works *even with plain surfaces*, including unpainted ceramics and architecture.

Data Capture: A turntable and a digital camera are used to acquire data from 670 viewpoints. For each viewpoint, we capture a set of images using illumination from four different flashes. Future embodiments will include a small, inexpensive handheld multi-flash camera



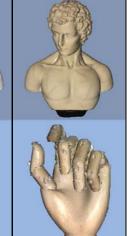
Multi-Flash Turntable Sequence: Input Image

Estimated Shape: 3D Point Cloud

Recovered Appearance: Phong BRDF Model







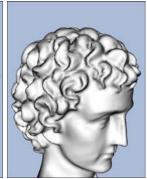
Recovering a Smooth Surface

The reconstructed point cloud can errors, including gaps and noise. To minimize these effects, we find an implicit surface which interpolates the 3D points. This method can be applied to any 3D point cloud, including those generated by laser scanners.



VFIso Results [2006 110x110x110 grid]











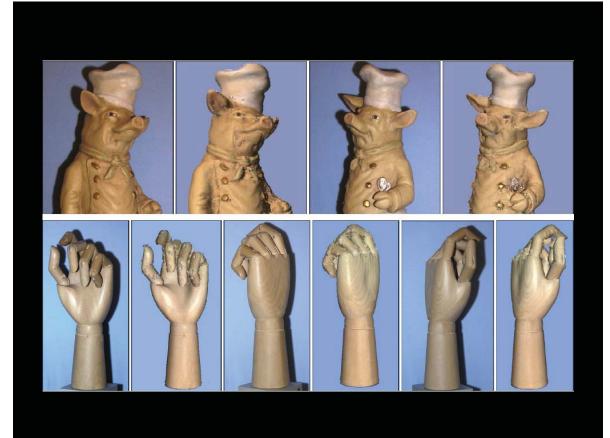












SSD Continuous Formulation

• Oriented point set:

$$D = \{ (\mathbf{p_i}, \mathbf{n_i}) \}$$
 sampled from a surface S

• Implicit surface:

$$S = \{ \mathbf{x} \mid f(\mathbf{x}) = 0 \}$$
 such that $f(\mathbf{p_i}) = 0$ and $\nabla f(\mathbf{p_i}) = \mathbf{n_i} \ \forall (\mathbf{p_i}, \mathbf{n_i}) \in D$

Least squares energy:

$$E(f) = \sum_{i=1}^{N} f(\mathbf{p_i})^2 + \lambda_1 \sum_{i=1}^{N} \|\nabla f(\mathbf{p_i}) - \mathbf{n_i}\|^2 + \lambda_2 \int_{V} \|Hf(\mathbf{x})\|^2 d\mathbf{x}$$

What does the regularization term do?

$$\frac{\lambda_0}{N} \sum_{i=1}^{N} f(p_i)^2 + \frac{\lambda_1}{N} \sum_{i=1}^{N} \|\nabla f(p_i) - n_i\|^2 + \frac{\lambda_2}{|V|} \int_{V} \|Hf(x)\|^2 dx$$

$$Hf(x) = \left[\frac{\partial \nabla f(x)}{\partial x_1} \frac{\partial \nabla f(x)}{\partial x_2} \frac{\partial \nabla f(x)}{\partial x_3} \right]$$

- Near data points: since the data terms dominate, the function approximates the signed distance
- Away from data points: the regularization term dominates and forces the gradient to be smooth and close to constant

Role of each energy term

$$E(f, v, M) = \sum_{i=1}^{N} f(\mathbf{p}_i)^2 + \lambda_1 \sum_{i=1}^{N} \|v(\mathbf{p}_i) - \mathbf{n}_i\|^2 + \lambda_2 \int_{V} \|M(\mathbf{x})\|^2 d\mathbf{x}$$

Quadratic energy in f, v, and M

If f, v, and M are linear functions of the same parameters, then the minimization reduces to a least squares problem

Linear families of functions

$$f(x) = \sum_{\alpha \in \Lambda} f_{\alpha} \, \phi_{\alpha}(x) = \Phi(x)^{t} F$$

- Popular Smooth Basis Functions
 - Monomials [Taubin'91]
 - Radial basis functions [Carr et al., '01],
 - Compactly supported basis functions [Othake et al. '04],
 - Trigonometric polynomials [Kazhdan et al. '05],
 - B-splines [Kazhdan et al., 06],
 - Wavelets [Manson et al. '08],

Non-homogenous, Quadratic energy

$$E(F) = F^t A F - 2b^t F + c$$

Global minimum

$$AF = b$$

We can use Independent Discretizations

- Hybrid FE/FD discretization
 - Trilinear interpolant for the function $f(\mathbf{x})$
 - Primal finite differences for the gradient $\nabla f(\mathbf{x})$
 - Dual finite differences for the Hessian $Hf(\mathbf{x})$
- As long as $f(\mathbf{x})$, $\nabla f(\mathbf{x})$, and $Hf(\mathbf{x})$ are written as a linear combinations of **the same** parameter vector F

Non-homogenous, Quadratic energy

$$E(F) = F^t A F - 2b^t F + c$$

Global minimum

$$AF = b$$

Implementation

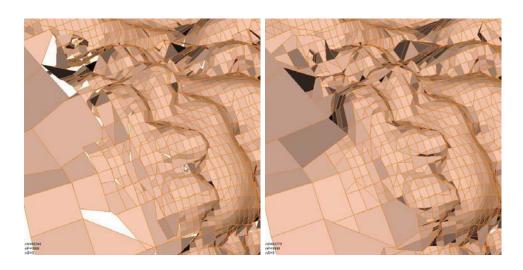
- Primal-Dual octree data structure
- Cascading multi-grid iterative solver (conjugate gradient):

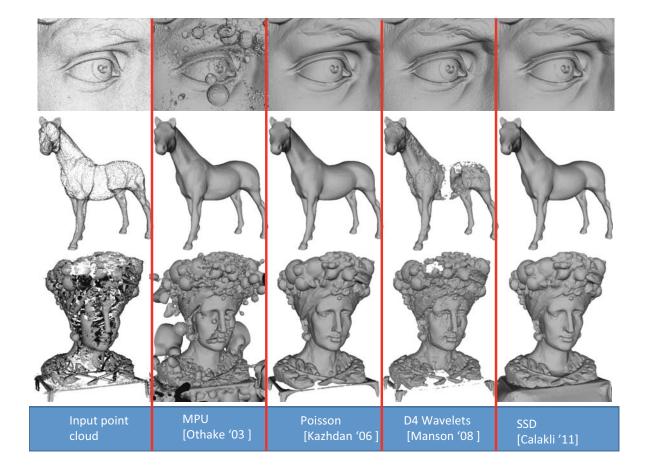
Solve the problem on a much coarser level

- Use the solution at that level to initialize the solution at the next level
- Refine with the iterative solver
- Iso-surface extraction (crack-free)
 - Dual marching cubes [Schaefer 2005]

Marching Cubes on Octrees

- Non-conforming hexahedral mesh
- Results in crack problem.
- Problem solved by Dual Marching Cubes





SSD Surface Reconstruction

- Theoretical contributions:
 - Oriented point samples regarded as samples of Euclidean signed distance function
 - Reconstruction as global minimization problem
 - Yet sparse system of linear equations
- Empirical advantages:
 - Robust to noise and uneven sampling density
- Future work:
 - Streaming out-of-core implementations
 - Parallel/Multi-core/GPU implementations
 - Dynamic shapes

Course Schedule

- Structured Lighting
- Projector-Camera Calibration
- Surface Reconstruction from Point Clouds
- > Elementary Mesh Processing
- Related Projects
- Conclusion / Q & A

Introducción a la Fotografia 3D UBA/FCEN Marzo 27 – Abril 12 2013 Clase 9 : Viernes Abril 12

Gabriel Taubin
Brown University

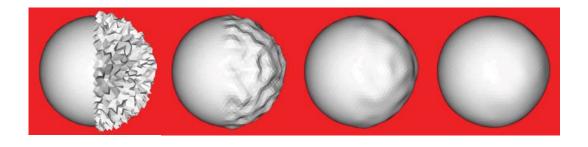


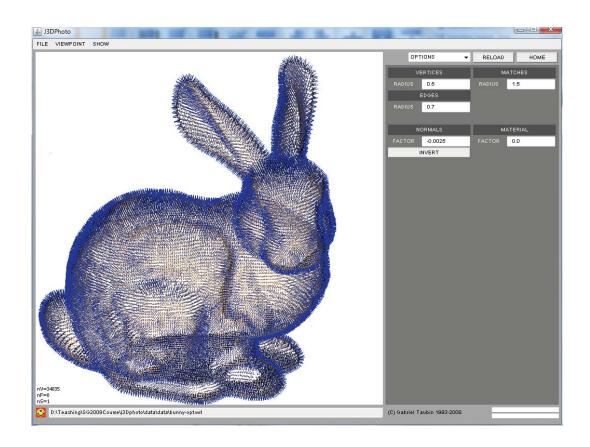
Course Schedule

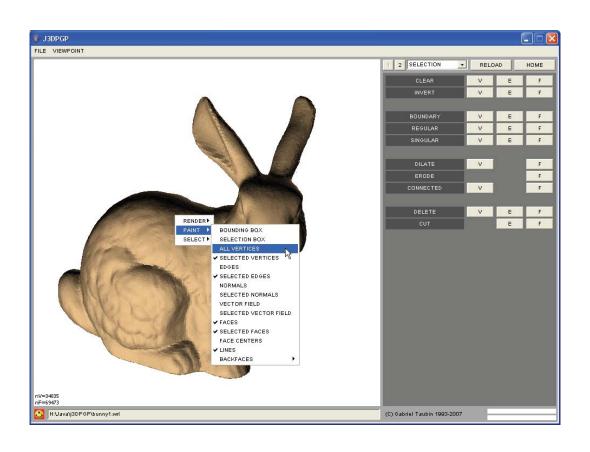
- Structured Lighting
- Projector Calibration / Structured Light Reconstruction
- Combining Point Clouds Recovered from Multiple Views
- Surface Reconstruction from Point Clouds
- Elementary Mesh Processing
- Related Projects
- Conclusion / Q & A

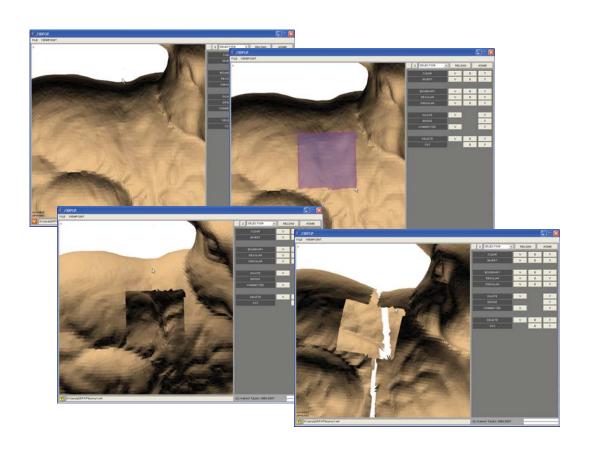
Elementary Mesh Processing

- We will talk about a few simple algorithms which can be applied interactively
- Polygon mesh smoothing / denoising
- Polygon mesh simplification
- j3DPGP (Java 3D Photography and Geometry Processing)

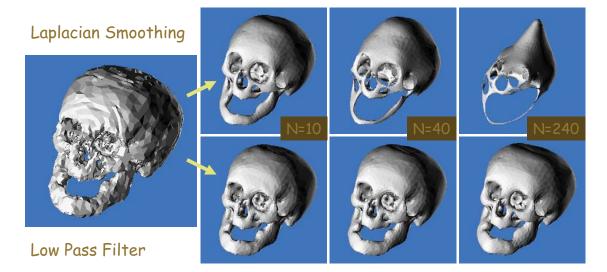








Polygon Mesh Smoothing / Denoising

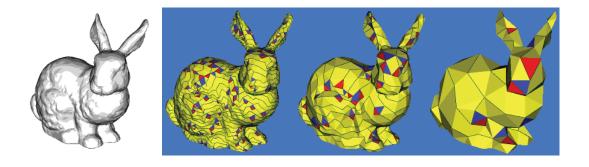


- Laplacian smoothing is the simplest smoothing/denoising algorithm
- Fix to shrinkage problem: toggle parameter sign at each iteration!

G. Taubin. A Signal Processing Approach To Fair Surface Design. Signraph. 1995

Poligon Mesh Simplification / Decimation

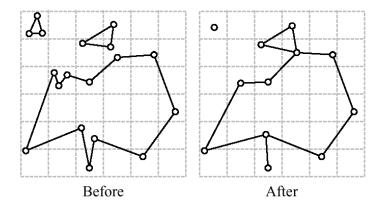
 Algorithms to reduce the number of vertices and faces while preserving geometric approximation to original shape



- Vertex clustering (Rossignac & Borrel, 1993)
- Edge Collapse (Garand Heckbert 1997; many others)

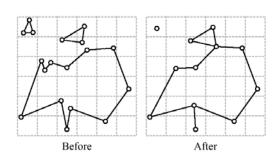
Vertex Clustering

- Quantize coordinates with respect to a bounding box
- Identify vertices with same coordinates
- Remove empty triangles



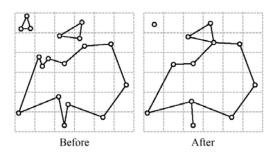
Vertex Clustering Algorithm

- Quantize coordinates with respect to bounding box
- Assign a new vertex index to each occupied cell
- · Determine coordinates of new vertices
- Construct new vertex index look-up table
- Replace vertex indices in faces
- Remove empty triangles from list of faces

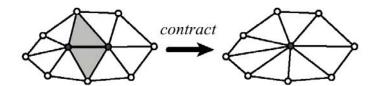


Vertex Clustering

- Advantages
 - Simple to implement
 - Works on large scenes with multiple objects
- No manifold restriction
- Disadvantages
 - Produces non-manifold meshes
 - Quality of simplified model is often not very good



Edge Collapse

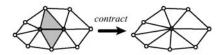


- Identify endpoints
- Determine vertex position
- Remove incident triangles
- Which edges to collapse?
- In which order?

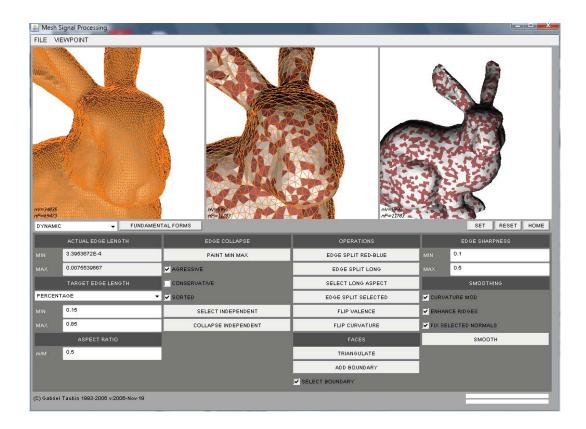
Non-existing edges

Before After

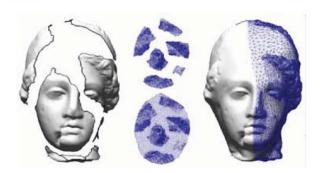
Basic Edge Collapse Algorithm

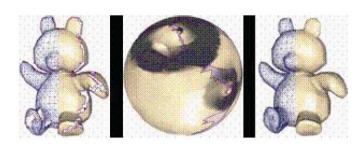


- Put all collapsible edges in a priority queue according to removal error
- · While queue is not empty
 - Delete minimum edge from queue
 - Collapse edge
 - Identify vertices
 - Remove all incident edges from the queue, determine if collapsible, recompute removal error, re-insert in queue
- Need dynamic data structures

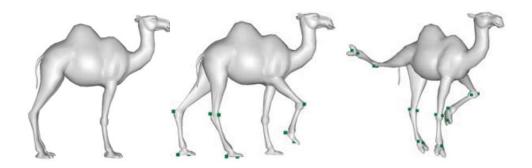




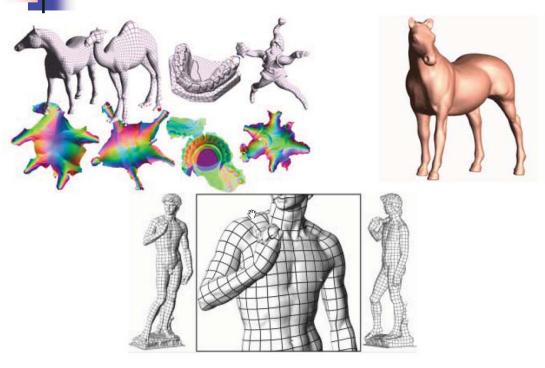


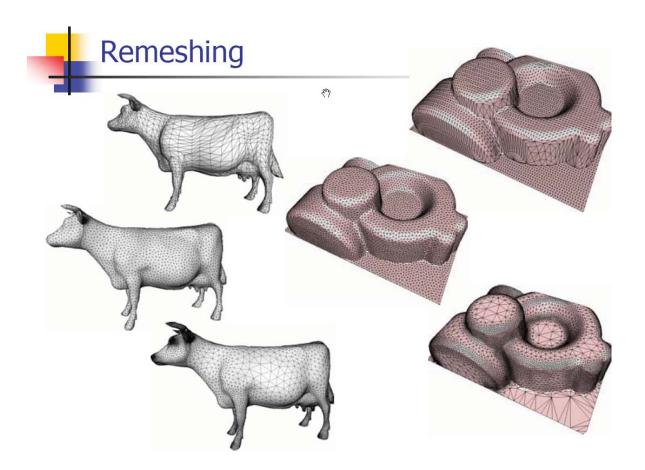


Deformation

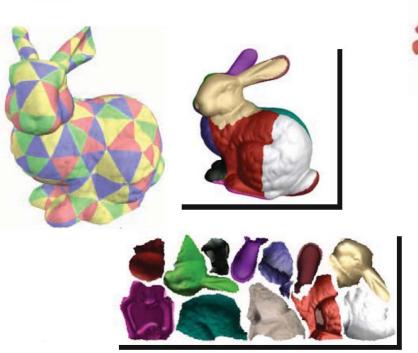


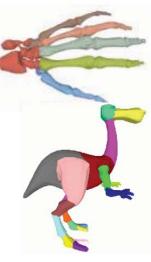












Course Schedule

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REVEAL Digital Archaeology Project

Cooper, Kimia, Taubin, Galor, Sanders, Willis

- Automates the tedious processes of data collection and documentation at the excavation site
- Provides visualization tools to explore the data collected in the database
- Solves specific problems in Archaeology using computer vision techniques
- Integrated Multi-View-Stereo (MVS) pipeline reconstructs 3D shapes from photos captured with hand-held cameras
- MVS pipeline can be installed independently of the rest of the system
- Software distributed as Open Source

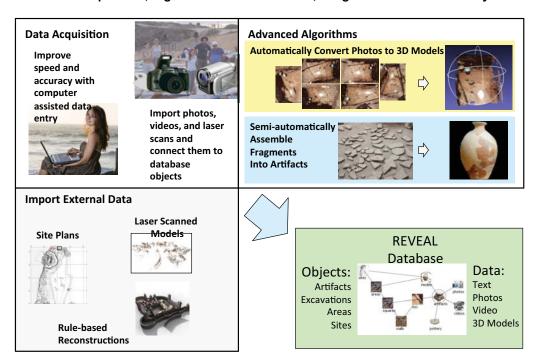
http://sourceforge.net/projects/revealanalyze/





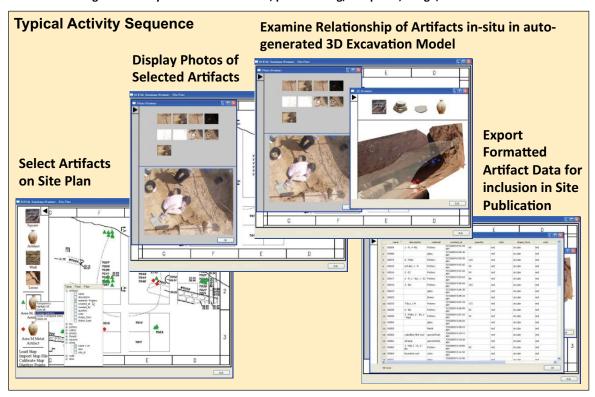
REVEAL Archaeological Data Acquisition

Assisted Data Acquisition, Algorithmic Reconstruction, Integrated multi-format analysis



REVEAL Archaeological Analysis

Data integrated and synchronized in tabular, plan drawing, 3D spatial, image, and video formats







Patch-based Multi-View Stereo (PMVS) http://grail.cs.washington.edu/software/pmvs/



[Furukawa and Ponce 2008]

Reconstruction of colored meshes

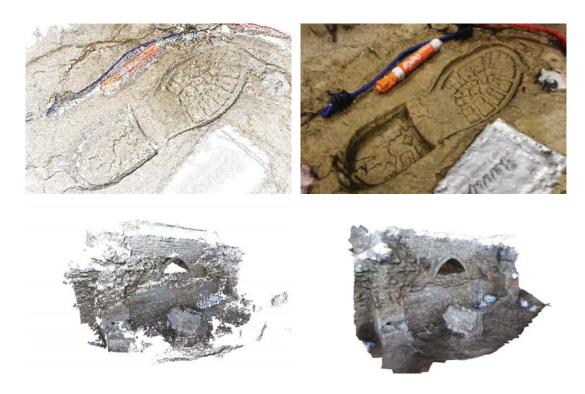


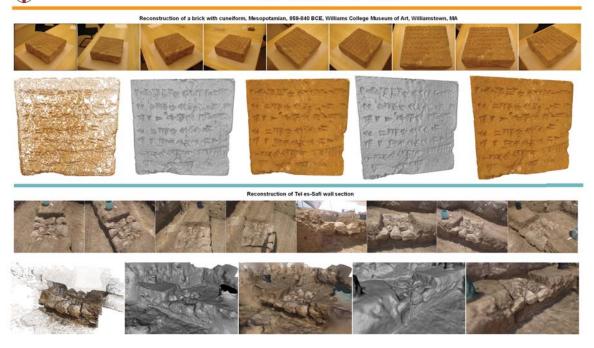


Fig. 1 Reconstruction of the side of a castle model: The input point cloud (top-left), Surface reconstructed by the proposed algorithm(top-right), Two views from the surface and color map reconstructed by the proposed algorithm (bottom).



High Resolution Surface and Appearance Modeling for Multi-view Stereo

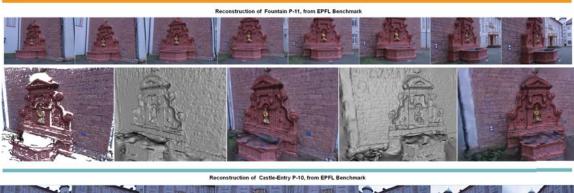
Fatih Calakli and Gabriel Taubin



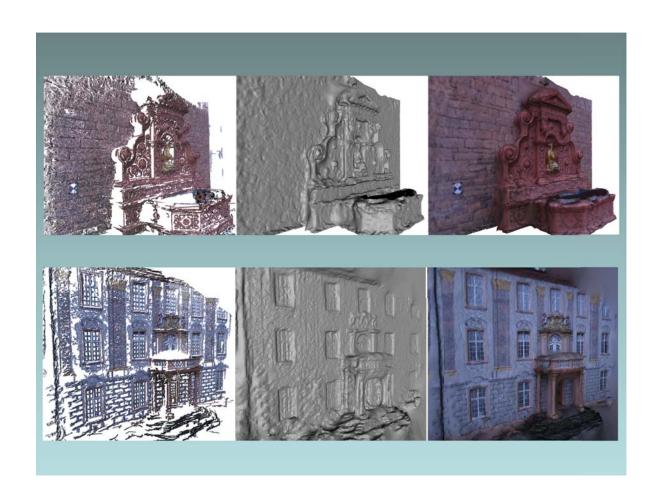


High Resolution Surface and Appearance Modeling for Multi-view Stereo

Fatih Calakli and Gabriel Taubin







From Multi-View Video Cameras



View Interpolation From Multi-View Video Cameras



With Background Segmentation

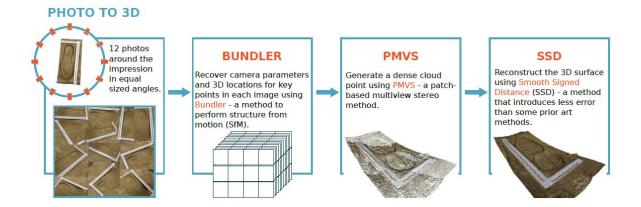


Ongoing work



Accurate 3D Footwear Impression Recovery From Photographs,

F. A. Andalo, F. Calakli, G. Taubin, and S. Goldenstein, International Conference on Imaging for Crime Detection and Prevention (ICDP-2011).



Comparable to 3D Laser Scanner

EXPERIMENTAL RESULTS





- d_g: Haursdoff distance map between the scanned shoe print and the scanned shoe sole.
- d_m: Haursdoff distance map between our 3D model and the scanned shoe sole.

Shoeprint #	$\overline{d_g}$	$\overline{d_m}$	$\overline{d_m} - \overline{d_g}$
1	9.996	10.002	0.006
2	8.157	8.660	0.503
3	8.715	9.480	0.765
4	8.816	9.114	0.298

(mm)

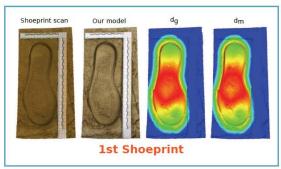
CONCLUSIONS

We presented a pipeline to recover footwear impressions from crime scenes using multiview stereo, which has not been considered for this kind of application until now.

Despite the simplicity, the obtained surfaces are comparable with 3D scanning.

Future work: more experiments number of images, angle between images, comparison with casting.

EXAMPLES



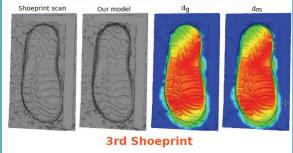
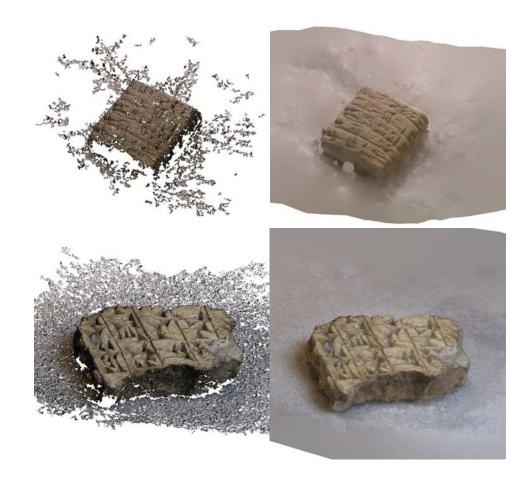
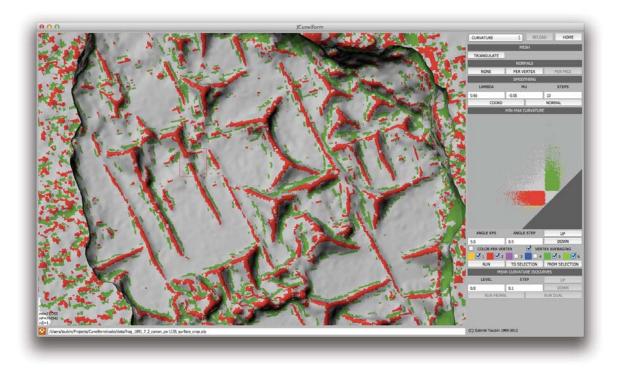




Fig. 6 Reconstruction of a brick with cuneiform, Mesopotamian, 859-840 BCE, clay, Overall $35 \times 35 \times 11$ cm, Williams College Museum of Art, Williamstown, MA, Gift of Professor Edgar J. Banks and Dr. John Henry Haynes, Class of 1876,(20.1.33.A). Top row: the input point cloud (left), and surface geometry (right) reconstructed by the proposed algorithm. Middle row: Two views from surface and color map reconstructed by the proposed algorithm. Bottom row: 6 examples from the set of 21 images that are used for shape acquisition.



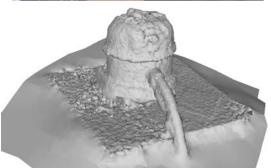


Handheld Interactive, Incremental 3D Object Scanning

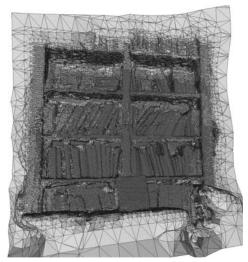
J. Kim & G. Taubin

- Based on MS Kinect sensor
- Continuous coarse pose estimation from color camera using PTAM
- 3D snapshots captured from different points of view using depth camera
- Alignment improced with Iterative Closest Points (ICP) algorithm
- SSD is run on aligned 3D snapshots











Real-Time High-Definition Stereo on GPGPU using Progressive Multi-Resolution Adaptive Windows

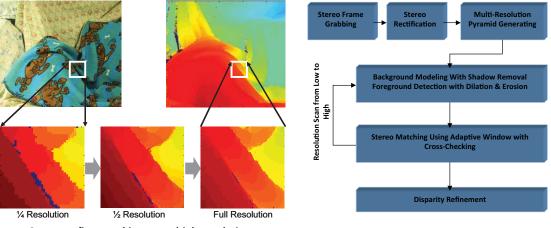
Y. Zhao, and G. Taubin, Image and Vision Computing 2011.



Screen shots of our real-time stereo system working on the field

Real-Time High-Definition Stereo on GPGPU using Progressive Multi-Resolution Adaptive Windows

Y. Zhao, and G. Taubin, Image and Vision Computing 2011.



Coarse-to-fine matching on multiple resolutions

Processing Pipeline

High Resolution Surface Reconstruction from Multi-view Aerial Imagery by Calakli, Ulusoy, Restrepo, Mundy & Taubin, 3DIMPVT 2012



Input Images Pro

Probabilistic Volumetric Modeling

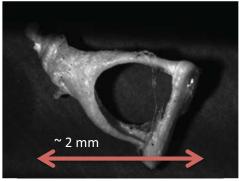
Surface Reconstruction

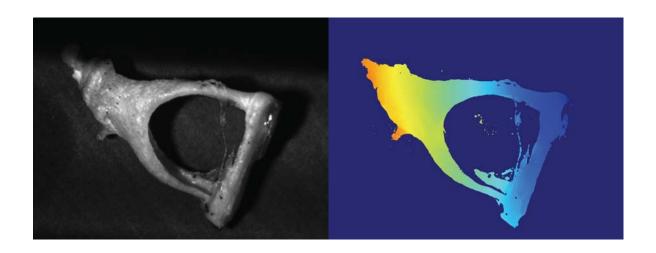
Microscopic 3D Shape Capture

Liberman & Taubin (work in progress)



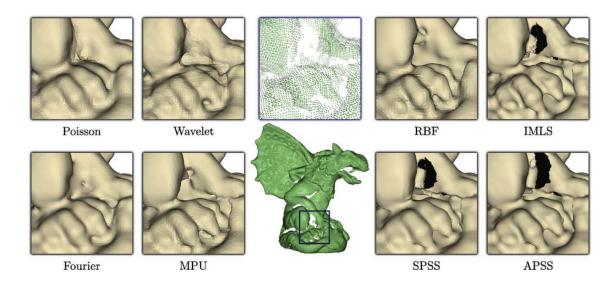






An Evaluation and Comparison of Surface Reconstruction

M. Berger, J. Levine, L. Nonato, C. Silva, and G. Taubin ACM Transactions on Graphics 2013 (Siggraph 2013)



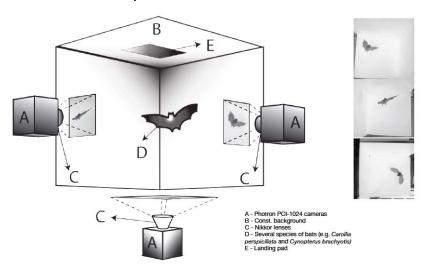
http://www.cs.utah.edu/~bergerm/recon_bench/

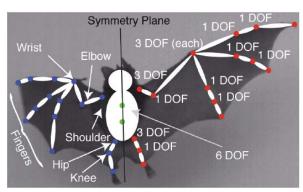
3D Reconstruction & Analysis of Bat Flight Maneuvers

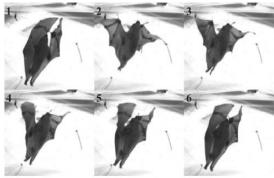
- 3D Reconstruction of Bat Flight Kinematics from Sparse Multiple Views, by A. Bergou, S. Swartz, and G. Taubin, and K. Breuer, 4DMOD, 2011.
- 3D Reconstruction and Analysis of Bat Flight Maneuvers from Sparse Multiple View Video, by A. Bergou, S. Swartz, S. K. Breuer, G. Taubin, BioVis, 2011.
- Falling with Style The Role of Wing Inertia in Bat Flight
 Maneuvers, by A. Bergou, D. Riskin, G. Taubin, S. Swartz, and
 K. Breuer, Annual Meeting, Society for Integrative and
 Comparative Biology, 2011.
- Falling with Style-Bat Flight Maneuvers, by A. Bergou, D. Riskin, G. Taubin, S. Swartz, and K. Breuer, Bulletin of the American Physical Society, Vol. 55, 2010.

How do we measure bats?

- Multiple synchronized 1000fps+ cameras
- Controlled environment (backdrop & illumination)
- Bats trained to land on landing pad
- Experiments with several species







- Bats have highly articulated wings
- Very complex wing motion
- Current goal: Detailed reconstruction of wing and body kinematics and derivatives from visual data
- Skeleton model with 52 degrees of freedom
- Geometry parameterized by 37 constants
- Future Goal: Model-less Dynamic Shape Reconstruction





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