

Modeling and Synthesis of Aperture Effects in Cameras

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- Introduction and Related Work
- Modeling Vignetting
- Synthesizing Vignetting
- Experimental Results
- Conclusions and Future Work

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Aperture Effects in Cameras

- While capturing all-in-focus images, small apertures (pinholes) are impractical due to limited exposures required by lighting or motion
- For larger apertures, *depth of field* effects are observed, including:
 (1) spatially-varying blur depending on depth, and (2) vignetting
- We present simple approaches to model and control these effects

Related Work



Radiometric Camera Calibration

- Source of non-idealities [Litvinov '05]
- "Flat-field" vignetting calib. [Yu '04]
- Single-image calib. [Zheng '06]
- Image mosaics [D'Angelo '07]

Coded-Aperture Imaging

- Useful for deblurring [Levin '07]
- Can be applied to capture light field photographs [Veeraraghavan '07]



Variable-Aperture Photography

- Aperture bracketing [Hasinoff '06]
- Confocal stereo [Hasinoff '07]

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Sources of Vignetting







Mechanical Vignetting:

- Due to physical obstructions (lens hoods, filters, etc.)
- Can completely block light from reaching certain regions

Optical Vignetting:

- Occurs in multi-element optical designs, due to decrease in clear area (exit pupil) off-axis
- Reduced using small apertures

Natural and Pixel Vignetting:

- Combines physics effects: (inverse-square fall-off of light, Lambert's law, foreshortening)
- Occlusion due to pixel depth

Geometric Model: Spatially-varying PSF

The distance **D** to the in-focus "object" plane for a thin lens is given by:

$$\frac{1}{f} = \frac{1}{f_D} + \frac{1}{D}$$

The image of an out-of-focus point at S will be a blurred region of width c, where:

$$c = \frac{|S-D|}{S} \cdot \frac{f^2}{N(D-f)}$$

- This model predicts that the PSF will scale according to the object distance S and the f-number N – requiring a calibration procedure to sample both parameters.
- However, as noted by Hasinoff and Kutulakos, the effective blur diameter *c* is given by the following linear relation.

$$\tilde{c} = \frac{|S - D|}{S}A$$



For this approximation, the spatiallyvarying PSF can be estimated from a single image, and is given by:

$$B_{\tilde{c}}(s,t;x,y) = \frac{1}{\tilde{c}^2} B_{\tilde{c}}\left(s,t;\frac{x}{\tilde{c}},\frac{y}{\tilde{c}}\right)$$

Photometric Model: Radial Intensity Fall-off



Photometric Vignetting Model

- As we have shown, various sources of vignetting result in a radial reduction in brightness that increases towards the image periphery
- Can be modeled as a low-order polynomial surface
- For known zoom, focal length, and aperture, traditional solution is to divide image intensity by a "flat-field" calibration image taken with a uniform white light area source (e.g., a light box)
- Unfortunately, this approach cannot simultaneously estimate the PSF

Experimental Vignetting Calibration

Calibration using Point Sources

- To obtain *simultaneous* estimates of the spatially-varying PSF and intensity fall-off, we use a point source array for calibration
- We observe that the image of a point light directly gives PSF (i.e., impulse response)
- Sparse PSFs → dense (i.e., per-pixel)
 PSFs using triangle-based interpolation





calibration pattern



"starophenperperpendicularia igneage

Experimental Vignetting Calibration



Note: Gray kernels are images of point lights, red is linearly-interpolated

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Vignetting Synthesis: The Bokeh Brush

Goal:

- We desire the ability to control the spatially-varying PSF post-capture
- Since the spatially-varying PSF is related to the shape of out-of-focus points, this goal is equivalent to controlling *bokeh*
- We will develop a "*Bokeh Brush*"



examples of bokeh

Observation:

PSF and aperture are closely-connected...



Vignetting Synthesis: Superposition Principle

Superposition Principle

 For unit magnification, the recorded image irradiance *I_i(x,y)* at a pixel (*x,y*) is

$$I_i(x,y) = \iint_{\Omega} B(s,t;x,y) I_o(s,t) ds dt$$

where Ω is the domain of the image, $I_0(x,y)$ is the object plane irradiance, and B(s,t;x,y) is the spatially-varying PSF

We can express the PSF using N basis functions {*B_i(s,t;x,y)*}, such that

$$I_i(x,y) = \sum_{i=1}^N \lambda_i \iint_{\Omega} B_i(s,t;x,y) I_o(s,t) ds dt$$

 Since the PSF and aperture are directly related, we collect a sequence of basis images using the apertures {*A_i(s,t;x,y)*}

$$A(s,t;x,y) = \sum_{i=1}^{N} \lambda_i A_i(s,t;x,y)$$

 Basis images can be linearly-combined to synthesize the image for any aperture, so long as the basis is a good approximation







Aperture Superposition: Lens Modifications



- Canon EOS Digital Rebel XT with a Canon EF 100mm 1:1.28 Macro Lens
- Modified to allow manual insertion of aperture patterns directly into the plane of the iris (i.e., by removing the original lens diaphragm)

Aperture Superposition: Laboratory Results



Note: Synthesized "7-segment" images using aperture superposition

Bokeh Synthesis using PCA

Applying Principal Components Analysis:

- Although we have shown that images with different apertures can be linearly-combined, we still require an efficient basis
- One solution is to use a set of translated pinholes (equivalent to recording the incident light field)
- But, specialized bases can be used to achieve greater compression ratios...
- Here we develop a positive-valued PCA basis





training apertures

basis apertures from PCA

reconstruction results

Bokeh Synthesis using NMF

Applying Non-negative Matrix Factorization:

- Rather than normalizing PCA basis, we can find non-negative apertures directly using NMF
- NMF developed by Lee and Seung [1999] and involves iteratively-solving for *positive* basis
- NMF eliminates "open" and "bias" apertures used by PCA, reducing total number of apertures
- Unfortunately, NMF basis is not unique





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Spatially-varying Deblurring



original image



uniformly-defocused image



deblurred (mean PSF)



deblurred (spatially-varying PSF)

- Example of simulated spatially-varying blur (i.e., invariant to scene depth)
- Deblurred with estimate of spatially-varying PSF from proposed method

Vignetting Synthesis: Simulated Results



simulated PCA basis images



synthesized apertures

Example of "Bokeh Brush" post-capture stylization, where the aperture function has been re-synthesized to represent each letter of the capitalized Arial font using a PCA-derived basis set

Vignetting Synthesis: Simulated Results



original HDR image

first PCA basis aperture

bokeh stylization

Example of "Bokeh Brush" post-capture stylization, where the aperture function has been re-synthesized in a spatially-varying manner to read "BOKEH" along the left wall from a PCA basis set

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Conclusions and Future Work

Contributions

- Applied the fact that the out-of-focus image of a point light directly gives the point spread function – leading to a practical, low-cost method to simultaneously estimate vignetting and spatially-varying point spread function
- Introduced the Bokeh Brush: a novel, post-capture method for full-resolution control of the shape of out-of-focus points – achieved using a small set of images with varying basis aperture shapes

Limitations of the Calibration Procedure

- Point sources require long exposures and only provide sparse PSFs
- The point light source array is assumed to be uniform, but LCDs can vary

Limitation of the Bokeh Brush

- Can only reconstruct apertures well-approximated by chosen basis
- Achieves only modest compression ratios for included examples

Future Work

Apply *Bokeh Brush* directly to light field photographs (i.e., pinhole basis set)